

Mathematica 11.3 Integration Test Results

on the problems in the test-suite directory "2 Exponentials"

Test results for the 98 problems in "2.1 u (F^(c (a+b x)))^n.m"

Test results for the 93 problems in "2.2 (c+d x)^m (F^(g (e+f x)))^n (a+b (F^(g (e+f x))))^p.m"

Problem 46: Unable to integrate problem.

$$\int \frac{(c + d x)^3}{a + b (F^g (e + f x))^n} dx$$

Optimal (type 4, 192 leaves, 6 steps):

$$\frac{(c + d x)^4}{4 a d} - \frac{(c + d x)^3 \operatorname{Log}\left[1 + \frac{b (F^g (e + f x))^n}{a}\right]}{a f g n \operatorname{Log}[F]} - \frac{3 d (c + d x)^2 \operatorname{PolyLog}\left[2, -\frac{b (F^g (e + f x))^n}{a}\right]}{a f^2 g^2 n^2 \operatorname{Log}[F]^2} +$$
$$\frac{6 d^2 (c + d x) \operatorname{PolyLog}\left[3, -\frac{b (F^g (e + f x))^n}{a}\right]}{a f^3 g^3 n^3 \operatorname{Log}[F]^3} - \frac{6 d^3 \operatorname{PolyLog}\left[4, -\frac{b (F^g (e + f x))^n}{a}\right]}{a f^4 g^4 n^4 \operatorname{Log}[F]^4}$$

Result (type 8, 27 leaves):

$$\int \frac{(c + d x)^3}{a + b (F^g (e + f x))^n} dx$$

Problem 47: Unable to integrate problem.

$$\int \frac{(c + d x)^2}{a + b (F^g (e + f x))^n} dx$$

Optimal (type 4, 145 leaves, 5 steps):

$$\frac{(c+dx)^3}{3ad} - \frac{(c+dx)^2 \operatorname{Log}\left[1 + \frac{b(Fg(e+fx))^n}{a}\right]}{afgn \operatorname{Log}[F]} - \frac{2d(c+dx) \operatorname{PolyLog}\left[2, -\frac{b(Fg(e+fx))^n}{a}\right]}{af^2g^2n^2 \operatorname{Log}[F]^2} + \frac{2d^2 \operatorname{PolyLog}\left[3, -\frac{b(Fg(e+fx))^n}{a}\right]}{af^3g^3n^3 \operatorname{Log}[F]^3}$$

Result (type 8, 27 leaves):

$$\int \frac{(c+dx)^2}{a+b(Fg(e+fx))^n} dx$$

Problem 48: Attempted integration timed out after 120 seconds.

$$\int \frac{c+dx}{a+b(Fg(e+fx))^n} dx$$

Optimal (type 4, 98 leaves, 4 steps):

$$\frac{(c+dx)^2}{2ad} - \frac{(c+dx) \operatorname{Log}\left[1 + \frac{b(Fg(e+fx))^n}{a}\right]}{afgn \operatorname{Log}[F]} - \frac{d \operatorname{PolyLog}\left[2, -\frac{b(Fg(e+fx))^n}{a}\right]}{af^2g^2n^2 \operatorname{Log}[F]^2}$$

Result (type 1, 1 leaves):

???

Problem 49: Result more than twice size of optimal antiderivative.

$$\int \frac{1}{a+b(Fg(e+fx))^n} dx$$

Optimal (type 3, 40 leaves, 5 steps):

$$\frac{x}{a} - \frac{\operatorname{Log}[a+b(Fg(e+fx))^n]}{afgn \operatorname{Log}[F]}$$

Result (type 3, 100 leaves):

$$\frac{x}{a} - \frac{\operatorname{Log}\left[a+b e^{n(-fgx \operatorname{Log}[F] + \operatorname{Log}[F^{e g - f g x}])}\right] (F e g + f g x)^{n - \frac{n(-fgx \operatorname{Log}[F] + \operatorname{Log}[F^{e g - f g x}])}{\operatorname{Log}[F^{e g - f g x}]}}}{afgn \operatorname{Log}[F]}$$

Problem 52: Unable to integrate problem.

$$\int \frac{(c+dx)^3}{(a+b(Fg(e+fx))^n)^2} dx$$

Optimal (type 4, 388 leaves, 13 steps):

$$\begin{aligned} & \frac{(c+dx)^4}{4a^2d} - \frac{(c+dx)^3}{a^2fgn\log[F]} + \frac{(c+dx)^3}{af(a+b(Fg^{e+fx}))^n g n \log[F]} + \frac{3d(c+dx)^2 \log\left[1 + \frac{b(Fg^{e+fx})^n}{a}\right]}{a^2f^2g^2n^2\log[F]^2} - \\ & \frac{(c+dx)^3 \log\left[1 + \frac{b(Fg^{e+fx})^n}{a}\right]}{a^2fgn\log[F]} + \frac{6d^2(c+dx) \operatorname{PolyLog}\left[2, -\frac{b(Fg^{e+fx})^n}{a}\right]}{a^2f^3g^3n^3\log[F]^3} - \frac{3d(c+dx)^2 \operatorname{PolyLog}\left[2, -\frac{b(Fg^{e+fx})^n}{a}\right]}{a^2f^2g^2n^2\log[F]^2} - \\ & \frac{6d^3 \operatorname{PolyLog}\left[3, -\frac{b(Fg^{e+fx})^n}{a}\right]}{a^2f^4g^4n^4\log[F]^4} + \frac{6d^2(c+dx) \operatorname{PolyLog}\left[3, -\frac{b(Fg^{e+fx})^n}{a}\right]}{a^2f^3g^3n^3\log[F]^3} - \frac{6d^3 \operatorname{PolyLog}\left[4, -\frac{b(Fg^{e+fx})^n}{a}\right]}{a^2f^4g^4n^4\log[F]^4} \end{aligned}$$

Result (type 8, 27 leaves):

$$\int \frac{(c+dx)^3}{(a+b(Fg^{e+fx}))^n} dx$$

Problem 53: Unable to integrate problem.

$$\int \frac{(c+dx)^2}{(a+b(Fg^{e+fx}))^n} dx$$

Optimal (type 4, 294 leaves, 11 steps):

$$\begin{aligned} & \frac{(c+dx)^3}{3a^2d} - \frac{(c+dx)^2}{a^2fgn\log[F]} + \frac{(c+dx)^2}{af(a+b(Fg^{e+fx}))^n g n \log[F]} + \frac{2d(c+dx) \log\left[1 + \frac{b(Fg^{e+fx})^n}{a}\right]}{a^2f^2g^2n^2\log[F]^2} - \\ & \frac{(c+dx)^2 \log\left[1 + \frac{b(Fg^{e+fx})^n}{a}\right]}{a^2fgn\log[F]} + \frac{2d^2 \operatorname{PolyLog}\left[2, -\frac{b(Fg^{e+fx})^n}{a}\right]}{a^2f^3g^3n^3\log[F]^3} - \frac{2d(c+dx) \operatorname{PolyLog}\left[2, -\frac{b(Fg^{e+fx})^n}{a}\right]}{a^2f^2g^2n^2\log[F]^2} + \frac{2d^2 \operatorname{PolyLog}\left[3, -\frac{b(Fg^{e+fx})^n}{a}\right]}{a^2f^3g^3n^3\log[F]^3} \end{aligned}$$

Result (type 8, 27 leaves):

$$\int \frac{(c+dx)^2}{(a+b(Fg^{e+fx}))^n} dx$$

Problem 54: Attempted integration timed out after 120 seconds.

$$\int \frac{c+dx}{(a+b(Fg^{e+fx}))^n} dx$$

Optimal (type 4, 191 leaves, 11 steps):

$$\frac{(c+dx)^2}{2a^2d} - \frac{dx}{a^2fgn\text{Log}[F]} + \frac{c+dx}{af(a+b(F^{fg(e+fx)})^n)gn\text{Log}[F]} + \frac{d\text{Log}[a+b(F^{fg(e+fx)})^n]}{a^2f^2g^2n^2\text{Log}[F]^2} - \frac{(c+dx)\text{Log}\left[1+\frac{b(F^{fg(e+fx)})^n}{a}\right]}{a^2fgn\text{Log}[F]} - \frac{d\text{PolyLog}\left[2, -\frac{b(F^{fg(e+fx)})^n}{a}\right]}{a^2f^2g^2n^2\text{Log}[F]^2}$$

Result (type 1, 1 leaves):

???

Problem 58: Unable to integrate problem.

$$\int \frac{(c+dx)^3}{(a+b(F^{fg(e+fx)})^n)^3} dx$$

Optimal (type 4, 594 leaves, 26 steps):

$$\begin{aligned} & \frac{(c+dx)^4}{4a^3d} + \frac{3d(c+dx)^2}{2a^3f^2g^2n^2\text{Log}[F]^2} - \frac{3d(c+dx)^2}{2a^2f^2(a+b(F^{fg(e+fx)})^n)g^2n^2\text{Log}[F]^2} - \frac{3(c+dx)^3}{2a^3fgn\text{Log}[F]} + \frac{(c+dx)^3}{2af(a+b(F^{fg(e+fx)})^n)^2gn\text{Log}[F]} + \\ & \frac{(c+dx)^3}{a^2f(a+b(F^{fg(e+fx)})^n)gn\text{Log}[F]} - \frac{3d^2(c+dx)\text{Log}\left[1+\frac{b(F^{fg(e+fx)})^n}{a}\right]}{a^3f^3g^3n^3\text{Log}[F]^3} + \frac{9d(c+dx)^2\text{Log}\left[1+\frac{b(F^{fg(e+fx)})^n}{a}\right]}{2a^3f^2g^2n^2\text{Log}[F]^2} - \frac{(c+dx)^3\text{Log}\left[1+\frac{b(F^{fg(e+fx)})^n}{a}\right]}{a^3fgn\text{Log}[F]} - \\ & \frac{3d^3\text{PolyLog}\left[2, -\frac{b(F^{fg(e+fx)})^n}{a}\right]}{a^3f^4g^4n^4\text{Log}[F]^4} + \frac{9d^2(c+dx)\text{PolyLog}\left[2, -\frac{b(F^{fg(e+fx)})^n}{a}\right]}{a^3f^3g^3n^3\text{Log}[F]^3} - \frac{3d(c+dx)^2\text{PolyLog}\left[2, -\frac{b(F^{fg(e+fx)})^n}{a}\right]}{a^3f^2g^2n^2\text{Log}[F]^2} - \\ & \frac{9d^3\text{PolyLog}\left[3, -\frac{b(F^{fg(e+fx)})^n}{a}\right]}{a^3f^4g^4n^4\text{Log}[F]^4} + \frac{6d^2(c+dx)\text{PolyLog}\left[3, -\frac{b(F^{fg(e+fx)})^n}{a}\right]}{a^3f^3g^3n^3\text{Log}[F]^3} - \frac{6d^3\text{PolyLog}\left[4, -\frac{b(F^{fg(e+fx)})^n}{a}\right]}{a^3f^4g^4n^4\text{Log}[F]^4} \end{aligned}$$

Result (type 8, 27 leaves):

$$\int \frac{(c+dx)^3}{(a+b(F^{fg(e+fx)})^n)^3} dx$$

Problem 59: Unable to integrate problem.

$$\int \frac{(c+dx)^2}{(a+b(F^{fg(e+fx)})^n)^3} dx$$

Optimal (type 4, 439 leaves, 24 steps):

$$\begin{aligned} & \frac{(c+dx)^3}{3a^3d} + \frac{d^2x}{a^3f^2g^2n^2\text{Log}[F]^2} - \frac{d(c+dx)}{a^2f^2(a+b(Fg^{(e+fx)}))^n g^2n^2\text{Log}[F]^2} - \frac{3(c+dx)^2}{2a^3fgn\text{Log}[F]} + \frac{(c+dx)^2}{2af(a+b(Fg^{(e+fx)}))^n g^2n\text{Log}[F]} + \\ & \frac{(c+dx)^2}{a^2f(a+b(Fg^{(e+fx)}))^n g^2n\text{Log}[F]} - \frac{d^2\text{Log}[a+b(Fg^{(e+fx)})^n]}{a^3f^3g^3n^3\text{Log}[F]^3} + \frac{3d(c+dx)\text{Log}\left[1+\frac{b(Fg^{(e+fx)})^n}{a}\right]}{a^3f^2g^2n^2\text{Log}[F]^2} - \frac{(c+dx)^2\text{Log}\left[1+\frac{b(Fg^{(e+fx)})^n}{a}\right]}{a^3fgn\text{Log}[F]} + \\ & \frac{3d^2\text{PolyLog}\left[2, -\frac{b(Fg^{(e+fx)})^n}{a}\right]}{a^3f^3g^3n^3\text{Log}[F]^3} - \frac{2d(c+dx)\text{PolyLog}\left[2, -\frac{b(Fg^{(e+fx)})^n}{a}\right]}{a^3f^2g^2n^2\text{Log}[F]^2} + \frac{2d^2\text{PolyLog}\left[3, -\frac{b(Fg^{(e+fx)})^n}{a}\right]}{a^3f^3g^3n^3\text{Log}[F]^3} \end{aligned}$$

Result (type 8, 27 leaves):

$$\int \frac{(c+dx)^2}{(a+b(Fg^{(e+fx)}))^3} dx$$

Problem 60: Attempted integration timed out after 120 seconds.

$$\int \frac{c+dx}{(a+b(Fg^{(e+fx)}))^3} dx$$

Optimal (type 4, 276 leaves, 17 steps):

$$\begin{aligned} & \frac{(c+dx)^2}{2a^3d} - \frac{d}{2a^2f^2(a+b(Fg^{(e+fx)}))^n g^2n^2\text{Log}[F]^2} - \frac{3dx}{2a^3fgn\text{Log}[F]} + \frac{c+dx}{2af(a+b(Fg^{(e+fx)}))^n g^2n\text{Log}[F]} + \\ & \frac{c+dx}{a^2f(a+b(Fg^{(e+fx)}))^n g^2n\text{Log}[F]} + \frac{3d\text{Log}[a+b(Fg^{(e+fx)})^n]}{2a^3f^2g^2n^2\text{Log}[F]^2} - \frac{(c+dx)\text{Log}\left[1+\frac{b(Fg^{(e+fx)})^n}{a}\right]}{a^3fgn\text{Log}[F]} - \frac{d\text{PolyLog}\left[2, -\frac{b(Fg^{(e+fx)})^n}{a}\right]}{a^3f^2g^2n^2\text{Log}[F]^2} \end{aligned}$$

Result (type 1, 1 leaves):

???

Problem 70: Unable to integrate problem.

$$\int (a+b(Fg^{(e+fx)}))^3 (c+dx)^m dx$$

Optimal (type 4, 340 leaves, 8 steps):

$$\frac{a^3 (c+dx)^{1+m}}{d(1+m)} + \frac{3^{-1-m} b^3 F^3 \left(e^{-\frac{cf}{d}} g^{n-3} g^n (e+fx) \right) (F e^{g+fgx})^{3n} (c+dx)^m \text{Gamma}\left[1+m, -\frac{3fgn(c+dx)\text{Log}[F]}{d}\right] \left(-\frac{fgn(c+dx)\text{Log}[F]}{d}\right)^{-m}}{fgn\text{Log}[F]} + \frac{1}{fgn\text{Log}[F]}$$

$$3 \times 2^{-1-m} a b^2 F^2 \left(e^{-\frac{cf}{d}} g^{n-2} g^n (e+fx) \right) (F e^{g+fgx})^{2n} (c+dx)^m \text{Gamma}\left[1+m, -\frac{2fgn(c+dx)\text{Log}[F]}{d}\right] \left(-\frac{fgn(c+dx)\text{Log}[F]}{d}\right)^{-m} +$$

$$\frac{3 a^2 b F \left(e^{-\frac{cf}{d}} g^{n-g^n} (e+fx) \right) (F e^{g+fgx})^n (c+dx)^m \text{Gamma}\left[1+m, -\frac{fgn(c+dx)\text{Log}[F]}{d}\right] \left(-\frac{fgn(c+dx)\text{Log}[F]}{d}\right)^{-m}}{fgn\text{Log}[F]}$$

Result (type 8, 27 leaves):

$$\int (a+b(Fg^{(e+fx)})^n)^3 (c+dx)^m dx$$

Problem 71: Unable to integrate problem.

$$\int (a+b(Fg^{(e+fx)})^n)^2 (c+dx)^m dx$$

Optimal (type 4, 228 leaves, 6 steps):

$$\frac{a^2 (c+dx)^{1+m}}{d(1+m)} + \frac{2^{-1-m} b^2 F^2 \left(e^{-\frac{cf}{d}} g^{n-2} g^n (e+fx) \right) (F e^{g+fgx})^{2n} (c+dx)^m \text{Gamma}\left[1+m, -\frac{2fgn(c+dx)\text{Log}[F]}{d}\right] \left(-\frac{fgn(c+dx)\text{Log}[F]}{d}\right)^{-m}}{fgn\text{Log}[F]} +$$

$$\frac{2 a b F \left(e^{-\frac{cf}{d}} g^{n-g^n} (e+fx) \right) (F e^{g+fgx})^n (c+dx)^m \text{Gamma}\left[1+m, -\frac{fgn(c+dx)\text{Log}[F]}{d}\right] \left(-\frac{fgn(c+dx)\text{Log}[F]}{d}\right)^{-m}}{fgn\text{Log}[F]}$$

Result (type 8, 27 leaves):

$$\int (a+b(Fg^{(e+fx)})^n)^2 (c+dx)^m dx$$

Problem 72: Unable to integrate problem.

$$\int (a+b(Fg^{(e+fx)})^n) (c+dx)^m dx$$

Optimal (type 4, 116 leaves, 4 steps):

$$\frac{a (c+dx)^{1+m}}{d(1+m)} + \frac{b F \left(e^{-\frac{cf}{d}} g^{n-g^n} (e+fx) \right) (F e^{g+fgx})^n (c+dx)^m \text{Gamma}\left[1+m, -\frac{fgn(c+dx)\text{Log}[F]}{d}\right] \left(-\frac{fgn(c+dx)\text{Log}[F]}{d}\right)^{-m}}{fgn\text{Log}[F]}$$

Result (type 8, 25 leaves):

$$\int (a + b (F^g (e+f x))^n) (c + d x)^m dx$$

Test results for the 774 problems in "2.3 Exponential functions.m"

Problem 16: Unable to integrate problem.

$$\int (F^{e (c+dx)})^n (a + b (F^{e (c+dx)})^n)^p dx$$

Optimal (type 3, 41 leaves, 2 steps):

$$\frac{(a + b (F^{e (c+dx)})^n)^{1+p}}{b d e n (1+p) \text{Log}[F]}$$

Result (type 8, 31 leaves):

$$\int (F^{e (c+dx)})^n (a + b (F^{e (c+dx)})^n)^p dx$$

Problem 17: Unable to integrate problem.

$$\int (a + b (F^{e (c+dx)})^n)^p (G^h (f+g x))^{\frac{d e n \text{Log}[F]}{g h \text{Log}[G]}} dx$$

Optimal (type 3, 80 leaves, 3 steps):

$$\frac{(F^{e (c+dx)})^{-n} (a + b (F^{e (c+dx)})^n)^{1+p} (G^h (f+g x))^{\frac{d e n \text{Log}[F]}{g h \text{Log}[G]}}}{b d e n (1+p) \text{Log}[F]}$$

Result (type 8, 46 leaves):

$$\int (a + b (F^{e (c+dx)})^n)^p (G^h (f+g x))^{\frac{d e n \text{Log}[F]}{g h \text{Log}[G]}} dx$$

Problem 39: Result more than twice size of optimal antiderivative.

$$\int \frac{e^x}{1 - e^{2x}} dx$$

Optimal (type 3, 4 leaves, 2 steps):

$$\text{ArcTanh}[e^x]$$

Result (type 3, 23 leaves):

$$-\frac{1}{2} \operatorname{Log}[1 - e^x] + \frac{1}{2} \operatorname{Log}[1 + e^x]$$

Problem 80: Result more than twice size of optimal antiderivative.

$$\int \frac{f^{a+bx^2}}{x^9} dx$$

Optimal (type 4, 24 leaves, 1 step):

$$-\frac{1}{2} b^4 f^a \operatorname{Gamma}[-4, -bx^2 \operatorname{Log}[f]] \operatorname{Log}[f]^4$$

Result (type 4, 71 leaves):

$$\frac{f^a \left(b^4 x^8 \operatorname{ExpIntegralEi}[bx^2 \operatorname{Log}[f]] \operatorname{Log}[f]^4 - f^{bx^2} (6 + 2bx^2 \operatorname{Log}[f] + b^2 x^4 \operatorname{Log}[f]^2 + b^3 x^6 \operatorname{Log}[f]^3) \right)}{48 x^8}$$

Problem 81: Result more than twice size of optimal antiderivative.

$$\int \frac{f^{a+bx^2}}{x^{11}} dx$$

Optimal (type 4, 24 leaves, 1 step):

$$\frac{1}{2} b^5 f^a \operatorname{Gamma}[-5, -bx^2 \operatorname{Log}[f]] \operatorname{Log}[f]^5$$

Result (type 4, 83 leaves):

$$\frac{1}{240 x^{10}} f^a \left(b^5 x^{10} \operatorname{ExpIntegralEi}[bx^2 \operatorname{Log}[f]] \operatorname{Log}[f]^5 - f^{bx^2} (24 + 6bx^2 \operatorname{Log}[f] + 2b^2 x^4 \operatorname{Log}[f]^2 + b^3 x^6 \operatorname{Log}[f]^3 + b^4 x^8 \operatorname{Log}[f]^4) \right)$$

Problem 82: Result more than twice size of optimal antiderivative.

$$\int f^{a+bx^2} x^{12} dx$$

Optimal (type 4, 34 leaves, 1 step):

$$-\frac{f^a x^{13} \operatorname{Gamma}\left[\frac{13}{2}, -bx^2 \operatorname{Log}[f]\right]}{2 \left(-bx^2 \operatorname{Log}[f]\right)^{13/2}}$$

Result (type 4, 119 leaves):

$$\frac{1}{128 b^{13/2} \text{Log}[f]^{13/2}} f^a \left(10395 \sqrt{\pi} \text{Erfi}[\sqrt{b} x \sqrt{\text{Log}[f]}] + 2 \sqrt{b} f^{b x^2} x \sqrt{\text{Log}[f]} \left(-10395 + 6930 b x^2 \text{Log}[f] - 2772 b^2 x^4 \text{Log}[f]^2 + 792 b^3 x^6 \text{Log}[f]^3 - 176 b^4 x^8 \text{Log}[f]^4 + 32 b^5 x^{10} \text{Log}[f]^5 \right) \right)$$

Problem 83: Result more than twice size of optimal antiderivative.

$$\int f^{a+b x^2} x^{10} dx$$

Optimal (type 4, 34 leaves, 1 step):

$$-\frac{f^a x^{11} \text{Gamma}\left[\frac{11}{2}, -b x^2 \text{Log}[f]\right]}{2 \left(-b x^2 \text{Log}[f]\right)^{11/2}}$$

Result (type 4, 107 leaves):

$$\frac{1}{64 b^{11/2} \text{Log}[f]^{11/2}} f^a \left(-945 \sqrt{\pi} \text{Erfi}[\sqrt{b} x \sqrt{\text{Log}[f]}] + 2 \sqrt{b} f^{b x^2} x \sqrt{\text{Log}[f]} \left(945 - 630 b x^2 \text{Log}[f] + 252 b^2 x^4 \text{Log}[f]^2 - 72 b^3 x^6 \text{Log}[f]^3 + 16 b^4 x^8 \text{Log}[f]^4 \right) \right)$$

Problem 93: Result more than twice size of optimal antiderivative.

$$\int \frac{f^{a+b x^2}}{x^{10}} dx$$

Optimal (type 4, 34 leaves, 1 step):

$$-\frac{f^a \text{Gamma}\left[-\frac{9}{2}, -b x^2 \text{Log}[f]\right] \left(-b x^2 \text{Log}[f]\right)^{9/2}}{2 x^9}$$

Result (type 4, 101 leaves):

$$\frac{1}{945 x^9} f^a \left(16 b^{9/2} \sqrt{\pi} x^9 \text{Erfi}[\sqrt{b} x \sqrt{\text{Log}[f]}] \text{Log}[f]^{9/2} - f^{b x^2} \left(105 + 30 b x^2 \text{Log}[f] + 12 b^2 x^4 \text{Log}[f]^2 + 8 b^3 x^6 \text{Log}[f]^3 + 16 b^4 x^8 \text{Log}[f]^4 \right) \right)$$

Problem 94: Result more than twice size of optimal antiderivative.

$$\int \frac{f^{a+b x^2}}{x^{12}} dx$$

Optimal (type 4, 34 leaves, 1 step):

$$-\frac{f^a \text{Gamma}\left[-\frac{11}{2}, -b x^2 \text{Log}[f]\right] (-b x^2 \text{Log}[f])^{11/2}}{2 x^{11}}$$

Result (type 4, 113 leaves):

$$\frac{1}{10395 x^{11}} f^a \left(32 b^{11/2} \sqrt{\pi} x^{11} \text{Erfi}\left[\sqrt{b} x \sqrt{\text{Log}[f]}\right] \text{Log}[f]^{11/2} - f^{b x^2} \left(945 + 210 b x^2 \text{Log}[f] + 60 b^2 x^4 \text{Log}[f]^2 + 24 b^3 x^6 \text{Log}[f]^3 + 16 b^4 x^8 \text{Log}[f]^4 + 32 b^5 x^{10} \text{Log}[f]^5 \right) \right)$$

Problem 106: Result more than twice size of optimal antiderivative.

$$\int \frac{f^{a+b x^3}}{x^{13}} dx$$

Optimal (type 4, 24 leaves, 1 step):

$$-\frac{1}{3} b^4 f^a \text{Gamma}\left[-4, -b x^3 \text{Log}[f]\right] \text{Log}[f]^4$$

Result (type 4, 71 leaves):

$$\frac{f^a \left(b^4 x^{12} \text{ExpIntegralEi}\left[b x^3 \text{Log}[f]\right] \text{Log}[f]^4 - f^{b x^3} \left(6 + 2 b x^3 \text{Log}[f] + b^2 x^6 \text{Log}[f]^2 + b^3 x^9 \text{Log}[f]^3 \right) \right)}{72 x^{12}}$$

Problem 107: Result more than twice size of optimal antiderivative.

$$\int \frac{f^{a+b x^3}}{x^{16}} dx$$

Optimal (type 4, 24 leaves, 1 step):

$$\frac{1}{3} b^5 f^a \text{Gamma}\left[-5, -b x^3 \text{Log}[f]\right] \text{Log}[f]^5$$

Result (type 4, 83 leaves):

$$\frac{1}{360 x^{15}} f^a \left(b^5 x^{15} \text{ExpIntegralEi}\left[b x^3 \text{Log}[f]\right] \text{Log}[f]^5 - f^{b x^3} \left(24 + 6 b x^3 \text{Log}[f] + 2 b^2 x^6 \text{Log}[f]^2 + b^3 x^9 \text{Log}[f]^3 + b^4 x^{12} \text{Log}[f]^4 \right) \right)$$

Problem 116: Result more than twice size of optimal antiderivative.

$$\int f^{a+\frac{b}{x}} x^4 dx$$

Optimal (type 4, 22 leaves, 1 step):

$$-b^5 f^a \text{Gamma}\left[-5, -\frac{b \text{Log}[f]}{x}\right] \text{Log}[f]^5$$

Result (type 4, 77 leaves):

$$\frac{1}{120} f^a \left(-b^5 \text{ExpIntegralEi}\left[\frac{b \text{Log}[f]}{x}\right] \text{Log}[f]^5 + f^{b/x} x \left(24 x^4 + 6 b x^3 \text{Log}[f] + 2 b^2 x^2 \text{Log}[f]^2 + b^3 x \text{Log}[f]^3 + b^4 \text{Log}[f]^4 \right) \right)$$

Problem 117: Result more than twice size of optimal antiderivative.

$$\int f^{a+\frac{b}{x}} x^3 dx$$

Optimal (type 4, 21 leaves, 1 step):

$$b^4 f^a \text{Gamma}\left[-4, -\frac{b \text{Log}[f]}{x}\right] \text{Log}[f]^4$$

Result (type 4, 65 leaves):

$$\frac{1}{24} f^a \left(-b^4 \text{ExpIntegralEi}\left[\frac{b \text{Log}[f]}{x}\right] \text{Log}[f]^4 + f^{b/x} x \left(6 x^3 + 2 b x^2 \text{Log}[f] + b^2 x \text{Log}[f]^2 + b^3 \text{Log}[f]^3 \right) \right)$$

Problem 129: Result more than twice size of optimal antiderivative.

$$\int f^{a+\frac{b}{x^2}} x^9 dx$$

Optimal (type 4, 24 leaves, 1 step):

$$-\frac{1}{2} b^5 f^a \text{Gamma}\left[-5, -\frac{b \text{Log}[f]}{x^2}\right] \text{Log}[f]^5$$

Result (type 4, 81 leaves):

$$\frac{1}{240} f^a \left(-b^5 \text{ExpIntegralEi}\left[\frac{b \text{Log}[f]}{x^2}\right] \text{Log}[f]^5 + f^{\frac{b}{x^2}} x^2 \left(24 x^8 + 6 b x^6 \text{Log}[f] + 2 b^2 x^4 \text{Log}[f]^2 + b^3 x^2 \text{Log}[f]^3 + b^4 \text{Log}[f]^4 \right) \right)$$

Problem 130: Result more than twice size of optimal antiderivative.

$$\int f^{a+\frac{b}{x^2}} x^7 dx$$

Optimal (type 4, 24 leaves, 1 step):

$$\frac{1}{2} b^4 f^a \text{Gamma}\left[-4, -\frac{b \text{Log}[f]}{x^2}\right] \text{Log}[f]^4$$

Result (type 4, 69 leaves):

$$\frac{1}{48} f^a \left(-b^4 \text{ExpIntegralEi} \left[\frac{b \text{Log}[f]}{x^2} \right] \text{Log}[f]^4 + f^{\frac{b}{x^2}} x^2 \left(6 x^6 + 2 b x^4 \text{Log}[f] + b^2 x^2 \text{Log}[f]^2 + b^3 \text{Log}[f]^3 \right) \right)$$

Problem 141: Result more than twice size of optimal antiderivative.

$$\int f^{a+\frac{b}{x^2}} x^{10} dx$$

Optimal (type 4, 34 leaves, 1 step):

$$\frac{1}{2} f^a x^{11} \text{Gamma} \left[-\frac{11}{2}, -\frac{b \text{Log}[f]}{x^2} \right] \left(-\frac{b \text{Log}[f]}{x^2} \right)^{11/2}$$

Result (type 4, 110 leaves):

$$\frac{1}{10395} f^a \left(-32 b^{11/2} \sqrt{\pi} \text{Erfi} \left[\frac{\sqrt{b} \sqrt{\text{Log}[f]}}{x} \right] \text{Log}[f]^{11/2} + f^{\frac{b}{x^2}} x \left(945 x^{10} + 210 b x^8 \text{Log}[f] + 60 b^2 x^6 \text{Log}[f]^2 + 24 b^3 x^4 \text{Log}[f]^3 + 16 b^4 x^2 \text{Log}[f]^4 + 32 b^5 \text{Log}[f]^5 \right) \right)$$

Problem 142: Result more than twice size of optimal antiderivative.

$$\int f^{a+\frac{b}{x^2}} x^8 dx$$

Optimal (type 4, 34 leaves, 1 step):

$$\frac{1}{2} f^a x^9 \text{Gamma} \left[-\frac{9}{2}, -\frac{b \text{Log}[f]}{x^2} \right] \left(-\frac{b \text{Log}[f]}{x^2} \right)^{9/2}$$

Result (type 4, 98 leaves):

$$\frac{1}{945} f^a \left(-16 b^{9/2} \sqrt{\pi} \text{Erfi} \left[\frac{\sqrt{b} \sqrt{\text{Log}[f]}}{x} \right] \text{Log}[f]^{9/2} + f^{\frac{b}{x^2}} x \left(105 x^8 + 30 b x^6 \text{Log}[f] + 12 b^2 x^4 \text{Log}[f]^2 + 8 b^3 x^2 \text{Log}[f]^3 + 16 b^4 \text{Log}[f]^4 \right) \right)$$

Problem 152: Result more than twice size of optimal antiderivative.

$$\int \frac{f^{a+\frac{b}{x^2}}}{x^{12}} dx$$

Optimal (type 4, 34 leaves, 1 step):

$$\frac{f^a \operatorname{Gamma}\left[\frac{11}{2}, -\frac{b \operatorname{Log}[f]}{x^2}\right]}{2 x^{11} \left(-\frac{b \operatorname{Log}[f]}{x^2}\right)^{11/2}}$$

Result (type 4, 112 leaves):

$$\frac{f^a \left(945 \sqrt{\pi} \operatorname{Erfi}\left[\frac{\sqrt{b} \sqrt{\operatorname{Log}[f]}}{x}\right] - \frac{2 \sqrt{b} f^{b/x^2} \sqrt{\operatorname{Log}[f]} (945 x^8 - 630 b x^6 \operatorname{Log}[f] + 252 b^2 x^4 \operatorname{Log}[f]^2 - 72 b^3 x^2 \operatorname{Log}[f]^3 + 16 b^4 \operatorname{Log}[f]^4)}{x^9} \right)}{64 b^{11/2} \operatorname{Log}[f]^{11/2}}$$

Problem 153: Result more than twice size of optimal antiderivative.

$$\int \frac{f^{a+\frac{b}{x^2}}}{x^{14}} dx$$

Optimal (type 4, 34 leaves, 1 step):

$$\frac{f^a \operatorname{Gamma}\left[\frac{13}{2}, -\frac{b \operatorname{Log}[f]}{x^2}\right]}{2 x^{13} \left(-\frac{b \operatorname{Log}[f]}{x^2}\right)^{13/2}}$$

Result (type 4, 124 leaves):

$$\frac{1}{128 b^{13/2} \operatorname{Log}[f]^{13/2}} f^a \left(-10395 \sqrt{\pi} \operatorname{Erfi}\left[\frac{\sqrt{b} \sqrt{\operatorname{Log}[f]}}{x}\right] + \frac{1}{x^{11}} \right. \\ \left. 2 \sqrt{b} f^{b/x^2} \sqrt{\operatorname{Log}[f]} (10395 x^{10} - 6930 b x^8 \operatorname{Log}[f] + 2772 b^2 x^6 \operatorname{Log}[f]^2 - 792 b^3 x^4 \operatorname{Log}[f]^3 + 176 b^4 x^2 \operatorname{Log}[f]^4 - 32 b^5 \operatorname{Log}[f]^5) \right)$$

Problem 155: Result more than twice size of optimal antiderivative.

$$\int f^{a+\frac{b}{x^3}} x^{14} dx$$

Optimal (type 4, 24 leaves, 1 step):

$$-\frac{1}{3} b^5 f^a \operatorname{Gamma}\left[-5, -\frac{b \operatorname{Log}[f]}{x^3}\right] \operatorname{Log}[f]^5$$

Result (type 4, 81 leaves):

$$\frac{1}{360} f^a \left(-b^5 \operatorname{ExpIntegralEi}\left[\frac{b \operatorname{Log}[f]}{x^3}\right] \operatorname{Log}[f]^5 + f^{b/x^3} x^3 (24 x^{12} + 6 b x^9 \operatorname{Log}[f] + 2 b^2 x^6 \operatorname{Log}[f]^2 + b^3 x^3 \operatorname{Log}[f]^3 + b^4 \operatorname{Log}[f]^4) \right)$$

Problem 156: Result more than twice size of optimal antiderivative.

$$\int f^{a+\frac{b}{x^3}} x^{11} dx$$

Optimal (type 4, 24 leaves, 1 step):

$$\frac{1}{3} b^4 f^a \text{Gamma}\left[-4, -\frac{b \text{Log}[f]}{x^3}\right] \text{Log}[f]^4$$

Result (type 4, 69 leaves):

$$\frac{1}{72} f^a \left(-b^4 \text{ExpIntegralEi}\left[\frac{b \text{Log}[f]}{x^3}\right] \text{Log}[f]^4 + f^{\frac{b}{x^3}} x^3 (6 x^9 + 2 b x^6 \text{Log}[f] + b^2 x^3 \text{Log}[f]^2 + b^3 \text{Log}[f]^3) \right)$$

Problem 202: Unable to integrate problem.

$$\int f^{c(a+bx)^3} x^2 dx$$

Optimal (type 4, 120 leaves, 5 steps):

$$\frac{f^{c(a+bx)^3}}{3 b^3 c \text{Log}[f]} + \frac{2 a (a+bx)^2 \text{Gamma}\left[\frac{2}{3}, -c(a+bx)^3 \text{Log}[f]\right]}{3 b^3 (-c(a+bx)^3 \text{Log}[f])^{2/3}} - \frac{a^2 (a+bx) \text{Gamma}\left[\frac{1}{3}, -c(a+bx)^3 \text{Log}[f]\right]}{3 b^3 (-c(a+bx)^3 \text{Log}[f])^{1/3}}$$

Result (type 8, 17 leaves):

$$\int f^{c(a+bx)^3} x^2 dx$$

Problem 203: Unable to integrate problem.

$$\int f^{c(a+bx)^3} x dx$$

Optimal (type 4, 92 leaves, 4 steps):

$$-\frac{(a+bx)^2 \text{Gamma}\left[\frac{2}{3}, -c(a+bx)^3 \text{Log}[f]\right]}{3 b^2 (-c(a+bx)^3 \text{Log}[f])^{2/3}} + \frac{a (a+bx) \text{Gamma}\left[\frac{1}{3}, -c(a+bx)^3 \text{Log}[f]\right]}{3 b^2 (-c(a+bx)^3 \text{Log}[f])^{1/3}}$$

Result (type 8, 15 leaves):

$$\int f^{c(a+bx)^3} x dx$$

Problem 208: Unable to integrate problem.

$$\int e^{a^3+3 a^2 b x+3 a b^2 x^2+b^3 x^3} x^4 dx$$

Optimal (type 4, 183 leaves, 8 steps):

$$\frac{2 a^2 e^{(a+b x)^3}}{b^5} - \frac{a^4 (a+b x) \operatorname{Gamma}\left[\frac{1}{3}, -(a+b x)^3\right]}{3 b^5 \left(-(a+b x)^3\right)^{1/3}} + \frac{4 a^3 (a+b x)^2 \operatorname{Gamma}\left[\frac{2}{3}, -(a+b x)^3\right]}{3 b^5 \left(-(a+b x)^3\right)^{2/3}} +$$

$$\frac{4 a (a+b x)^4 \operatorname{Gamma}\left[\frac{4}{3}, -(a+b x)^3\right]}{3 b^5 \left(-(a+b x)^3\right)^{4/3}} - \frac{(a+b x)^5 \operatorname{Gamma}\left[\frac{5}{3}, -(a+b x)^3\right]}{3 b^5 \left(-(a+b x)^3\right)^{5/3}}$$

Result (type 8, 35 leaves):

$$\int e^{a^3+3 a^2 b x+3 a b^2 x^2+b^3 x^3} x^4 dx$$

Problem 209: Unable to integrate problem.

$$\int e^{a^3+3 a^2 b x+3 a b^2 x^2+b^3 x^3} x^3 dx$$

Optimal (type 4, 138 leaves, 7 steps):

$$-\frac{a e^{(a+b x)^3}}{b^4} + \frac{a^3 (a+b x) \operatorname{Gamma}\left[\frac{1}{3}, -(a+b x)^3\right]}{3 b^4 \left(-(a+b x)^3\right)^{1/3}} - \frac{a^2 (a+b x)^2 \operatorname{Gamma}\left[\frac{2}{3}, -(a+b x)^3\right]}{b^4 \left(-(a+b x)^3\right)^{2/3}} - \frac{(a+b x)^4 \operatorname{Gamma}\left[\frac{4}{3}, -(a+b x)^3\right]}{3 b^4 \left(-(a+b x)^3\right)^{4/3}}$$

Result (type 8, 35 leaves):

$$\int e^{a^3+3 a^2 b x+3 a b^2 x^2+b^3 x^3} x^3 dx$$

Problem 210: Unable to integrate problem.

$$\int e^{a^3+3 a^2 b x+3 a b^2 x^2+b^3 x^3} x^2 dx$$

Optimal (type 4, 99 leaves, 6 steps):

$$\frac{e^{(a+b x)^3}}{3 b^3} - \frac{a^2 (a+b x) \operatorname{Gamma}\left[\frac{1}{3}, -(a+b x)^3\right]}{3 b^3 \left(-(a+b x)^3\right)^{1/3}} + \frac{2 a (a+b x)^2 \operatorname{Gamma}\left[\frac{2}{3}, -(a+b x)^3\right]}{3 b^3 \left(-(a+b x)^3\right)^{2/3}}$$

Result (type 8, 35 leaves):

$$\int e^{a^3+3 a^2 b x+3 a b^2 x^2+b^3 x^3} x^2 dx$$

Problem 211: Unable to integrate problem.

$$\int e^{a^3+3 a^2 b x+3 a b^2 x^2+b^3 x^3} x dx$$

Optimal (type 4, 80 leaves, 5 steps):

$$\frac{a (a + b x) \operatorname{Gamma}\left[\frac{1}{3}, -(a + b x)^3\right]}{3 b^2 \left(-(a + b x)^3\right)^{1/3}} - \frac{(a + b x)^2 \operatorname{Gamma}\left[\frac{2}{3}, -(a + b x)^3\right]}{3 b^2 \left(-(a + b x)^3\right)^{2/3}}$$

Result (type 8, 33 leaves):

$$\int e^{a^3+3 a^2 b x+3 a b^2 x^2+b^3 x^3} x dx$$

Problem 247: Unable to integrate problem.

$$\int f^{c (a+b x)^n} x^3 dx$$

Optimal (type 4, 207 leaves, 6 steps):

$$\begin{aligned} & - \frac{(a + b x)^4 \operatorname{Gamma}\left[\frac{4}{n}, -c (a + b x)^n \operatorname{Log}[f]\right] \left(-c (a + b x)^n \operatorname{Log}[f]\right)^{-4/n}}{b^4 n} + \frac{3 a (a + b x)^3 \operatorname{Gamma}\left[\frac{3}{n}, -c (a + b x)^n \operatorname{Log}[f]\right] \left(-c (a + b x)^n \operatorname{Log}[f]\right)^{-3/n}}{b^4 n} \\ & - \frac{3 a^2 (a + b x)^2 \operatorname{Gamma}\left[\frac{2}{n}, -c (a + b x)^n \operatorname{Log}[f]\right] \left(-c (a + b x)^n \operatorname{Log}[f]\right)^{-2/n}}{b^4 n} + \frac{a^3 (a + b x) \operatorname{Gamma}\left[\frac{1}{n}, -c (a + b x)^n \operatorname{Log}[f]\right] \left(-c (a + b x)^n \operatorname{Log}[f]\right)^{-1/n}}{b^4 n} \end{aligned}$$

Result (type 8, 17 leaves):

$$\int f^{c (a+b x)^n} x^3 dx$$

Problem 248: Unable to integrate problem.

$$\int f^{c (a+b x)^n} x^2 dx$$

Optimal (type 4, 154 leaves, 5 steps):

$$-\frac{(a+bx)^3 \text{Gamma}\left[\frac{3}{n}, -c(a+bx)^n \text{Log}[f]\right] (-c(a+bx)^n \text{Log}[f])^{-3/n}}{b^3 n} +$$

$$\frac{2a(a+bx)^2 \text{Gamma}\left[\frac{2}{n}, -c(a+bx)^n \text{Log}[f]\right] (-c(a+bx)^n \text{Log}[f])^{-2/n}}{b^3 n} - \frac{a^2(a+bx) \text{Gamma}\left[\frac{1}{n}, -c(a+bx)^n \text{Log}[f]\right] (-c(a+bx)^n \text{Log}[f])^{-1/n}}{b^3 n}$$

Result (type 8, 17 leaves):

$$\int f^{c(a+bx)^n} x^2 dx$$

Problem 265: Result more than twice size of optimal antiderivative.

$$\int \frac{F^{a+b(c+dx)^2}}{(c+dx)^9} dx$$

Optimal (type 4, 31 leaves, 1 step):

$$-\frac{b^4 F^a \text{Gamma}\left[-4, -b(c+dx)^2 \text{Log}[F]\right] \text{Log}[F]^4}{2d}$$

Result (type 4, 95 leaves):

$$\frac{1}{48d} F^a \left(b^4 \text{ExpIntegralEi}\left[b(c+dx)^2 \text{Log}[F]\right] \text{Log}[F]^4 - \frac{F^{b(c+dx)^2} \left(6 + 2b(c+dx)^2 \text{Log}[F] + b^2(c+dx)^4 \text{Log}[F]^2 + b^3(c+dx)^6 \text{Log}[F]^3\right)}{(c+dx)^8} \right)$$

Problem 266: Result more than twice size of optimal antiderivative.

$$\int \frac{F^{a+b(c+dx)^2}}{(c+dx)^{11}} dx$$

Optimal (type 4, 31 leaves, 1 step):

$$\frac{b^5 F^a \text{Gamma}\left[-5, -b(c+dx)^2 \text{Log}[F]\right] \text{Log}[F]^5}{2d}$$

Result (type 4, 111 leaves):

$$\frac{1}{240d} F^a \left(b^5 \text{ExpIntegralEi}\left[b(c+dx)^2 \text{Log}[F]\right] \text{Log}[F]^5 - \frac{1}{(c+dx)^{10}} \right.$$

$$\left. F^{b(c+dx)^2} \left(24 + 6b(c+dx)^2 \text{Log}[F] + 2b^2(c+dx)^4 \text{Log}[F]^2 + b^3(c+dx)^6 \text{Log}[F]^3 + b^4(c+dx)^8 \text{Log}[F]^4 \right) \right)$$

Problem 267: Result more than twice size of optimal antiderivative.

$$\int F^{a+b(c+dx)^2} (c+dx)^{12} dx$$

Optimal (type 4, 49 leaves, 1 step):

$$-\frac{F^a (c+dx)^{13} \text{Gamma}\left[\frac{13}{2}, -b(c+dx)^2 \text{Log}[F]\right]}{2d \left(-b(c+dx)^2 \text{Log}[F]\right)^{13/2}}$$

Result (type 4, 155 leaves):

$$\frac{1}{128 b^{13/2} d \text{Log}[F]^{13/2}} F^a \left(10395 \sqrt{\pi} \text{Erfi}\left[\sqrt{b}(c+dx) \sqrt{\text{Log}[F]}\right] - 2\sqrt{b} F^{b(c+dx)^2} \sqrt{\text{Log}[F]} \left(10395 (c+dx) - 6930 b (c+dx)^3 \text{Log}[F] + 2772 b^2 (c+dx)^5 \text{Log}[F]^2 - 792 b^3 (c+dx)^7 \text{Log}[F]^3 + 176 b^4 (c+dx)^9 \text{Log}[F]^4 - 32 b^5 (c+dx)^{11} \text{Log}[F]^5 \right) \right)$$

Problem 268: Result more than twice size of optimal antiderivative.

$$\int F^{a+b(c+dx)^2} (c+dx)^{10} dx$$

Optimal (type 4, 49 leaves, 1 step):

$$-\frac{F^a (c+dx)^{11} \text{Gamma}\left[\frac{11}{2}, -b(c+dx)^2 \text{Log}[F]\right]}{2d \left(-b(c+dx)^2 \text{Log}[F]\right)^{11/2}}$$

Result (type 4, 139 leaves):

$$\frac{1}{64 b^{11/2} d \text{Log}[F]^{11/2}} F^a \left(-945 \sqrt{\pi} \text{Erfi}\left[\sqrt{b}(c+dx) \sqrt{\text{Log}[F]}\right] + 2\sqrt{b} F^{b(c+dx)^2} \sqrt{\text{Log}[F]} \left(945 (c+dx) - 630 b (c+dx)^3 \text{Log}[F] + 252 b^2 (c+dx)^5 \text{Log}[F]^2 - 72 b^3 (c+dx)^7 \text{Log}[F]^3 + 16 b^4 (c+dx)^9 \text{Log}[F]^4 \right) \right)$$

Problem 278: Result more than twice size of optimal antiderivative.

$$\int \frac{F^{a+b(c+dx)^2}}{(c+dx)^{10}} dx$$

Optimal (type 4, 49 leaves, 1 step):

$$\frac{F^a \operatorname{Gamma}\left[-\frac{9}{2}, -b(c+dx)^2 \operatorname{Log}[F]\right] \left(-b(c+dx)^2 \operatorname{Log}[F]\right)^{9/2}}{2d(c+dx)^9}$$

Result (type 4, 129 leaves):

$$\frac{1}{945d} F^a \left(16b^{9/2} \sqrt{\pi} \operatorname{Erfi}\left[\sqrt{b}(c+dx) \sqrt{\operatorname{Log}[F]}\right] \operatorname{Log}[F]^{9/2} - \frac{1}{(c+dx)^9} F^{b(c+dx)^2} \left(105 + 30b(c+dx)^2 \operatorname{Log}[F] + 12b^2(c+dx)^4 \operatorname{Log}[F]^2 + 8b^3(c+dx)^6 \operatorname{Log}[F]^3 + 16b^4(c+dx)^8 \operatorname{Log}[F]^4 \right) \right)$$

Problem 279: Result more than twice size of optimal antiderivative.

$$\int \frac{F^{a+b(c+dx)^2}}{(c+dx)^{12}} dx$$

Optimal (type 4, 49 leaves, 1 step):

$$\frac{F^a \operatorname{Gamma}\left[-\frac{11}{2}, -b(c+dx)^2 \operatorname{Log}[F]\right] \left(-b(c+dx)^2 \operatorname{Log}[F]\right)^{11/2}}{2d(c+dx)^{11}}$$

Result (type 4, 152 leaves):

$$\frac{1}{10395d(c+dx)^{11}} F^a \left(32b^{11/2} \sqrt{\pi} (c+dx)^{11} \operatorname{Erfi}\left[\sqrt{b}(c+dx) \sqrt{\operatorname{Log}[F]}\right] \operatorname{Log}[F]^{11/2} - F^{b(c+dx)^2} \left(945 + 210b(c+dx)^2 \operatorname{Log}[F] + 60b^2(c+dx)^4 \operatorname{Log}[F]^2 + 24b^3(c+dx)^6 \operatorname{Log}[F]^3 + 16b^4(c+dx)^8 \operatorname{Log}[F]^4 + 32b^5(c+dx)^{10} \operatorname{Log}[F]^5 \right) \right)$$

Problem 291: Result more than twice size of optimal antiderivative.

$$\int \frac{F^{a+b(c+dx)^3}}{(c+dx)^{13}} dx$$

Optimal (type 4, 31 leaves, 1 step):

$$\frac{b^4 F^a \operatorname{Gamma}\left[-4, -b(c+dx)^3 \operatorname{Log}[F]\right] \operatorname{Log}[F]^4}{3d}$$

Result (type 4, 95 leaves):

$$\frac{1}{72d} F^a \left(b^4 \operatorname{ExpIntegralEi}\left[b(c+dx)^3 \operatorname{Log}[F]\right] \operatorname{Log}[F]^4 - \frac{F^{b(c+dx)^3} \left(6 + 2b(c+dx)^3 \operatorname{Log}[F] + b^2(c+dx)^6 \operatorname{Log}[F]^2 + b^3(c+dx)^9 \operatorname{Log}[F]^3 \right)}{(c+dx)^{12}} \right)$$

Problem 292: Result more than twice size of optimal antiderivative.

$$\int \frac{F^{a+b(c+dx)^3}}{(c+dx)^{16}} dx$$

Optimal (type 4, 31 leaves, 1 step):

$$\frac{b^5 F^a \text{Gamma}[-5, -b(c+dx)^3 \text{Log}[F]] \text{Log}[F]^5}{3d}$$

Result (type 4, 111 leaves):

$$\frac{1}{360d} F^a \left(b^5 \text{ExpIntegralEi}[b(c+dx)^3 \text{Log}[F]] \text{Log}[F]^5 - \frac{1}{(c+dx)^{15}} F^{b(c+dx)^3} \left(24 + 6b(c+dx)^3 \text{Log}[F] + 2b^2(c+dx)^6 \text{Log}[F]^2 + b^3(c+dx)^9 \text{Log}[F]^3 + b^4(c+dx)^{12} \text{Log}[F]^4 \right) \right)$$

Problem 302: Result more than twice size of optimal antiderivative.

$$\int F^{a+\frac{b}{c+dx}} (c+dx)^4 dx$$

Optimal (type 4, 29 leaves, 1 step):

$$-\frac{b^5 F^a \text{Gamma}[-5, -\frac{b \text{Log}[F]}{c+dx}] \text{Log}[F]^5}{d}$$

Result (type 4, 108 leaves):

$$\frac{1}{120d} F^a \left(-b^5 \text{ExpIntegralEi}\left[\frac{b \text{Log}[F]}{c+dx}\right] \text{Log}[F]^5 + F^{\frac{b}{c+dx}} (c+dx) \left(24(c+dx)^4 + 6b(c+dx)^3 \text{Log}[F] + 2b^2(c+dx)^2 \text{Log}[F]^2 + b^3(c+dx) \text{Log}[F]^3 + b^4 \text{Log}[F]^4 \right) \right)$$

Problem 303: Result more than twice size of optimal antiderivative.

$$\int F^{a+\frac{b}{c+dx}} (c+dx)^3 dx$$

Optimal (type 4, 28 leaves, 1 step):

$$\frac{b^4 F^a \text{Gamma}[-4, -\frac{b \text{Log}[F]}{c+dx}] \text{Log}[F]^4}{d}$$

Result (type 4, 92 leaves):

$$\frac{1}{24 d} F^a \left(-b^4 \text{ExpIntegralEi} \left[\frac{b \text{Log}[F]}{c+d x} \right] \text{Log}[F]^4 + F^{\frac{b}{c+d x}} (c+d x) \left(6 (c+d x)^3 + 2 b (c+d x)^2 \text{Log}[F] + b^2 (c+d x) \text{Log}[F]^2 + b^3 \text{Log}[F]^3 \right) \right)$$

Problem 315: Result more than twice size of optimal antiderivative.

$$\int F^{a+\frac{b}{(c+d x)^2}} (c+d x)^9 dx$$

Optimal (type 4, 31 leaves, 1 step):

$$\frac{b^5 F^a \text{Gamma} \left[-5, -\frac{b \text{Log}[F]}{(c+d x)^2} \right] \text{Log}[F]^5}{2 d}$$

Result (type 4, 112 leaves):

$$\frac{1}{240 d} F^a \left(-b^5 \text{ExpIntegralEi} \left[\frac{b \text{Log}[F]}{(c+d x)^2} \right] \text{Log}[F]^5 + F^{\frac{b}{(c+d x)^2}} (c+d x)^2 \left(24 (c+d x)^8 + 6 b (c+d x)^6 \text{Log}[F] + 2 b^2 (c+d x)^4 \text{Log}[F]^2 + b^3 (c+d x)^2 \text{Log}[F]^3 + b^4 \text{Log}[F]^4 \right) \right)$$

Problem 316: Result more than twice size of optimal antiderivative.

$$\int F^{a+\frac{b}{(c+d x)^2}} (c+d x)^7 dx$$

Optimal (type 4, 31 leaves, 1 step):

$$\frac{b^4 F^a \text{Gamma} \left[-4, -\frac{b \text{Log}[F]}{(c+d x)^2} \right] \text{Log}[F]^4}{2 d}$$

Result (type 4, 96 leaves):

$$\frac{1}{48 d} F^a \left(-b^4 \text{ExpIntegralEi} \left[\frac{b \text{Log}[F]}{(c+d x)^2} \right] \text{Log}[F]^4 + F^{\frac{b}{(c+d x)^2}} (c+d x)^2 \left(6 (c+d x)^6 + 2 b (c+d x)^4 \text{Log}[F] + b^2 (c+d x)^2 \text{Log}[F]^2 + b^3 \text{Log}[F]^3 \right) \right)$$

Problem 327: Result more than twice size of optimal antiderivative.

$$\int F^{a+\frac{b}{(c+d x)^2}} (c+d x)^{10} dx$$

Optimal (type 4, 49 leaves, 1 step):

$$\frac{F^a (c + d x)^{11} \text{Gamma}\left[-\frac{11}{2}, -\frac{b \text{Log}[F]}{(c+dx)^2}\right] \left(-\frac{b \text{Log}[F]}{(c+dx)^2}\right)^{11/2}}{2 d}$$

Result (type 4, 145 leaves):

$$\frac{1}{10395 d} F^a \left(-32 b^{11/2} \sqrt{\pi} \text{Erfi}\left[\frac{\sqrt{b} \sqrt{\text{Log}[F]}}{c + d x}\right] \text{Log}[F]^{11/2} + F^{\frac{b}{(c+dx)^2}} (c + d x) \right. \\ \left. (945 (c + d x)^{10} + 210 b (c + d x)^8 \text{Log}[F] + 60 b^2 (c + d x)^6 \text{Log}[F]^2 + 24 b^3 (c + d x)^4 \text{Log}[F]^3 + 16 b^4 (c + d x)^2 \text{Log}[F]^4 + 32 b^5 \text{Log}[F]^5) \right)$$

Problem 328: Result more than twice size of optimal antiderivative.

$$\int F^{a + \frac{b}{(c+dx)^2}} (c + d x)^8 dx$$

Optimal (type 4, 49 leaves, 1 step):

$$\frac{F^a (c + d x)^9 \text{Gamma}\left[-\frac{9}{2}, -\frac{b \text{Log}[F]}{(c+dx)^2}\right] \left(-\frac{b \text{Log}[F]}{(c+dx)^2}\right)^{9/2}}{2 d}$$

Result (type 4, 129 leaves):

$$\frac{1}{945 d} F^a \left(-16 b^{9/2} \sqrt{\pi} \text{Erfi}\left[\frac{\sqrt{b} \sqrt{\text{Log}[F]}}{c + d x}\right] \text{Log}[F]^{9/2} + \right. \\ \left. F^{\frac{b}{(c+dx)^2}} (c + d x) (105 (c + d x)^8 + 30 b (c + d x)^6 \text{Log}[F] + 12 b^2 (c + d x)^4 \text{Log}[F]^2 + 8 b^3 (c + d x)^2 \text{Log}[F]^3 + 16 b^4 \text{Log}[F]^4) \right)$$

Problem 338: Result more than twice size of optimal antiderivative.

$$\int \frac{F^{a + \frac{b}{(c+dx)^2}}}{(c + d x)^{12}} dx$$

Optimal (type 4, 49 leaves, 1 step):

$$\frac{F^a \text{Gamma}\left[\frac{11}{2}, -\frac{b \text{Log}[F]}{(c+dx)^2}\right]}{2 d (c + d x)^{11} \left(-\frac{b \text{Log}[F]}{(c+dx)^2}\right)^{11/2}}$$

Result (type 4, 143 leaves):

$$\frac{1}{64 b^{11/2} d \operatorname{Log}[F]^{11/2}} F^a \left(945 \sqrt{\pi} \operatorname{Erfi} \left[\frac{\sqrt{b} \sqrt{\operatorname{Log}[F]}}{c + d x} \right] - \frac{1}{(c + d x)^9} \right. \\ \left. 2 \sqrt{b} F^{\frac{b}{(c+dx)^2}} \sqrt{\operatorname{Log}[F]} \left(945 (c + d x)^8 - 630 b (c + d x)^6 \operatorname{Log}[F] + 252 b^2 (c + d x)^4 \operatorname{Log}[F]^2 - 72 b^3 (c + d x)^2 \operatorname{Log}[F]^3 + 16 b^4 \operatorname{Log}[F]^4 \right) \right)$$

Problem 339: Result more than twice size of optimal antiderivative.

$$\int \frac{F^{a + \frac{b}{(c+dx)^2}}}{(c + d x)^{14}} dx$$

Optimal (type 4, 49 leaves, 1 step):

$$\frac{F^a \operatorname{Gamma} \left[\frac{13}{2}, -\frac{b \operatorname{Log}[F]}{(c+dx)^2} \right]}{2 d (c + d x)^{13} \left(-\frac{b \operatorname{Log}[F]}{(c+dx)^2} \right)^{13/2}}$$

Result (type 4, 159 leaves):

$$\frac{1}{128 b^{13/2} d \operatorname{Log}[F]^{13/2}} F^a \left(-10395 \sqrt{\pi} \operatorname{Erfi} \left[\frac{\sqrt{b} \sqrt{\operatorname{Log}[F]}}{c + d x} \right] + \frac{1}{(c + d x)^{11}} 2 \sqrt{b} F^{\frac{b}{(c+dx)^2}} \sqrt{\operatorname{Log}[F]} \right. \\ \left. \left(10395 (c + d x)^{10} - 6930 b (c + d x)^8 \operatorname{Log}[F] + 2772 b^2 (c + d x)^6 \operatorname{Log}[F]^2 - 792 b^3 (c + d x)^4 \operatorname{Log}[F]^3 + 176 b^4 (c + d x)^2 \operatorname{Log}[F]^4 - 32 b^5 \operatorname{Log}[F]^5 \right) \right)$$

Problem 341: Result more than twice size of optimal antiderivative.

$$\int F^{a + \frac{b}{(c+dx)^3}} (c + d x)^{14} dx$$

Optimal (type 4, 31 leaves, 1 step):

$$\frac{b^5 F^a \operatorname{Gamma} \left[-5, -\frac{b \operatorname{Log}[F]}{(c+dx)^3} \right] \operatorname{Log}[F]^5}{3 d}$$

Result (type 4, 112 leaves):

$$\frac{1}{360 d} F^a \left(-b^5 \operatorname{ExpIntegralEi} \left[\frac{b \operatorname{Log}[F]}{(c + d x)^3} \right] \operatorname{Log}[F]^5 + \right. \\ \left. F^{\frac{b}{(c+dx)^3}} (c + d x)^3 \left(24 (c + d x)^{12} + 6 b (c + d x)^9 \operatorname{Log}[F] + 2 b^2 (c + d x)^6 \operatorname{Log}[F]^2 + b^3 (c + d x)^3 \operatorname{Log}[F]^3 + b^4 \operatorname{Log}[F]^4 \right) \right)$$

Problem 342: Result more than twice size of optimal antiderivative.

$$\int F^{a+\frac{b}{(c+dx)^3}} (c+dx)^{11} dx$$

Optimal (type 4, 31 leaves, 1 step):

$$\frac{b^4 F^a \text{Gamma}\left[-4, -\frac{b \text{Log}[F]}{(c+dx)^3}\right] \text{Log}[F]^4}{3 d}$$

Result (type 4, 96 leaves):

$$\frac{1}{72 d} F^a \left(-b^4 \text{ExpIntegralEi}\left[\frac{b \text{Log}[F]}{(c+dx)^3}\right] \text{Log}[F]^4 + F^{\frac{b}{(c+dx)^3}} (c+dx)^3 \left(6 (c+dx)^9 + 2 b (c+dx)^6 \text{Log}[F] + b^2 (c+dx)^3 \text{Log}[F]^2 + b^3 \text{Log}[F]^3 \right) \right)$$

Problem 359: Unable to integrate problem.

$$\int F^{a+b(c+dx)^n} (c+dx)^m dx$$

Optimal (type 4, 61 leaves, 1 step):

$$\frac{F^a (c+dx)^{1+m} \text{Gamma}\left[\frac{1+m}{n}, -b (c+dx)^n \text{Log}[F]\right] (-b (c+dx)^n \text{Log}[F])^{-\frac{1+m}{n}}}{d n}$$

Result (type 8, 23 leaves):

$$\int F^{a+b(c+dx)^n} (c+dx)^m dx$$

Problem 362: Unable to integrate problem.

$$\int F^{a+b(c+dx)^n} (c+dx) dx$$

Optimal (type 4, 54 leaves, 1 step):

$$\frac{F^a (c+dx)^2 \text{Gamma}\left[\frac{2}{n}, -b (c+dx)^n \text{Log}[F]\right] (-b (c+dx)^n \text{Log}[F])^{-2/n}}{d n}$$

Result (type 8, 21 leaves):

$$\int F^{a+b(c+dx)^n} (c+dx) dx$$

Problem 378: Result more than twice size of optimal antiderivative.

$$\int F^{a+b(c+dx)^n} (c+dx)^{-1-4n} dx$$

Optimal (type 4, 32 leaves, 1 step):

$$\frac{b^4 F^a \text{Gamma}[-4, -b(c+dx)^n \text{Log}[F]] \text{Log}[F]^4}{dn}$$

Result (type 4, 113 leaves):

$$\frac{1}{24 dn} F^a (c+dx)^{-4n} \left(b^4 (c+dx)^{4n} \text{ExpIntegralEi}[b(c+dx)^n \text{Log}[F]] \text{Log}[F]^4 - F^{b(c+dx)^n} \left(6 + 2b(c+dx)^n \text{Log}[F] + b^2 (c+dx)^{2n} \text{Log}[F]^2 + b^3 (c+dx)^{3n} \text{Log}[F]^3 \right) \right)$$

Problem 379: Result more than twice size of optimal antiderivative.

$$\int F^{a+b(c+dx)^n} (c+dx)^{-1-5n} dx$$

Optimal (type 4, 31 leaves, 1 step):

$$\frac{b^5 F^a \text{Gamma}[-5, -b(c+dx)^n \text{Log}[F]] \text{Log}[F]^5}{dn}$$

Result (type 4, 131 leaves):

$$\frac{1}{120 dn} F^a (c+dx)^{-5n} \left(b^5 (c+dx)^{5n} \text{ExpIntegralEi}[b(c+dx)^n \text{Log}[F]] \text{Log}[F]^5 - F^{b(c+dx)^n} \left(24 + 6b(c+dx)^n \text{Log}[F] + 2b^2 (c+dx)^{2n} \text{Log}[F]^2 + b^3 (c+dx)^{3n} \text{Log}[F]^3 + b^4 (c+dx)^{4n} \text{Log}[F]^4 \right) \right)$$

Problem 380: Unable to integrate problem.

$$\int F^{c+(a+bx)^n} (a+bx)^{-1+\frac{n}{2}} dx$$

Optimal (type 4, 47 leaves, 2 steps):

$$\frac{\sqrt{\pi} \text{Erfi}[\sqrt{c} (a+bx)^{n/2} \sqrt{\text{Log}[F]}]}{b \sqrt{c} n \sqrt{\text{Log}[F]}}$$

Result (type 8, 27 leaves):

$$\int F^{c (a+bx)^n} (a+bx)^{-1+\frac{n}{2}} dx$$

Problem 381: Unable to integrate problem.

$$\int F^{-c (a+bx)^n} (a+bx)^{-1+\frac{n}{2}} dx$$

Optimal (type 4, 47 leaves, 2 steps):

$$\frac{\sqrt{\pi} \operatorname{Erf}\left[\sqrt{c} (a+bx)^{n/2} \sqrt{\operatorname{Log}[F]}\right]}{b \sqrt{c} n \sqrt{\operatorname{Log}[F]}}$$

Result (type 8, 28 leaves):

$$\int F^{-c (a+bx)^n} (a+bx)^{-1+\frac{n}{2}} dx$$

Problem 391: Unable to integrate problem.

$$\int e^{e (c+dx)^3} (a+bx)^3 dx$$

Optimal (type 4, 177 leaves, 6 steps):

$$-\frac{b^2 (bc - ad) e^{e (c+dx)^3}}{d^4 e} + \frac{(bc - ad)^3 (c+dx) \operatorname{Gamma}\left[\frac{1}{3}, -e (c+dx)^3\right]}{3 d^4 (-e (c+dx)^3)^{1/3}} - \frac{b (bc - ad)^2 (c+dx)^2 \operatorname{Gamma}\left[\frac{2}{3}, -e (c+dx)^3\right]}{d^4 (-e (c+dx)^3)^{2/3}} - \frac{b^3 (c+dx)^4 \operatorname{Gamma}\left[\frac{4}{3}, -e (c+dx)^3\right]}{3 d^4 (-e (c+dx)^3)^{4/3}}$$

Result (type 8, 21 leaves):

$$\int e^{e (c+dx)^3} (a+bx)^3 dx$$

Problem 392: Unable to integrate problem.

$$\int e^{e (c+dx)^3} (a+bx)^2 dx$$

Optimal (type 4, 126 leaves, 5 steps):

$$\frac{b^2 e^{e(c+dx)^3}}{3d^3 e} - \frac{(bc-ad)^2 (c+dx) \text{Gamma}\left[\frac{1}{3}, -e(c+dx)^3\right]}{3d^3 (-e(c+dx)^3)^{1/3}} + \frac{2b(bc-ad)(c+dx)^2 \text{Gamma}\left[\frac{2}{3}, -e(c+dx)^3\right]}{3d^3 (-e(c+dx)^3)^{2/3}}$$

Result (type 8, 21 leaves):

$$\int e^{e(c+dx)^3} (a+bx)^2 dx$$

Problem 393: Unable to integrate problem.

$$\int e^{e(c+dx)^3} (a+bx) dx$$

Optimal (type 4, 92 leaves, 4 steps):

$$\frac{(bc-ad)(c+dx) \text{Gamma}\left[\frac{1}{3}, -e(c+dx)^3\right]}{3d^2 (-e(c+dx)^3)^{1/3}} - \frac{b(c+dx)^2 \text{Gamma}\left[\frac{2}{3}, -e(c+dx)^3\right]}{3d^2 (-e(c+dx)^3)^{2/3}}$$

Result (type 8, 19 leaves):

$$\int e^{e(c+dx)^3} (a+bx) dx$$

Problem 399: Unable to integrate problem.

$$\int \frac{F^{a+\frac{b}{c+dx}}}{(e+fx)^3} dx$$

Optimal (type 4, 267 leaves, 18 steps):

$$\frac{d^2 F^{a+\frac{b}{c+dx}}}{2f(de-cf)^2} - \frac{F^{a+\frac{b}{c+dx}}}{2f(e+fx)^2} - \frac{bd^2 F^{a+\frac{b}{c+dx}} \text{Log}[F]}{2(de-cf)^3} + \frac{bd F^{a+\frac{b}{c+dx}} \text{Log}[F]}{2(de-cf)^2(e+fx)} - \frac{bd^2 F^{a-\frac{bf}{de-cf}} \text{ExpIntegralEi}\left[\frac{bd(e+fx) \text{Log}[F]}{(de-cf)(c+dx)}\right] \text{Log}[F]}{(de-cf)^3} + \frac{b^2 d^2 f F^{a-\frac{bf}{de-cf}} \text{ExpIntegralEi}\left[\frac{bd(e+fx) \text{Log}[F]}{(de-cf)(c+dx)}\right] \text{Log}[F]^2}{2(de-cf)^4}$$

Result (type 8, 23 leaves):

$$\int \frac{F^{a+\frac{b}{c+dx}}}{(e+fx)^3} dx$$

Problem 400: Unable to integrate problem.

$$\int \frac{F^{a+\frac{b}{c+dx}}}{(e+fx)^4} dx$$

Optimal (type 4, 460 leaves, 36 steps):

$$\begin{aligned} & \frac{d^3 F^{a+\frac{b}{c+dx}}}{3f(de-cf)^3} - \frac{F^{a+\frac{b}{c+dx}}}{3f(e+fx)^3} - \frac{5bd^3 F^{a+\frac{b}{c+dx}} \operatorname{Log}[F]}{6(de-cf)^4} + \frac{bd F^{a+\frac{b}{c+dx}} \operatorname{Log}[F]}{6(de-cf)^2(e+fx)^2} + \frac{2bd^2 F^{a+\frac{b}{c+dx}} \operatorname{Log}[F]}{3(de-cf)^3(e+fx)} - \\ & \frac{bd^3 F^{a-\frac{bf}{de-cf}} \operatorname{ExpIntegralEi}\left[\frac{bd(e+fx)\operatorname{Log}[F]}{(de-cf)(c+dx)}\right] \operatorname{Log}[F]}{(de-cf)^4} + \frac{b^2 d^3 f F^{a+\frac{b}{c+dx}} \operatorname{Log}[F]^2}{6(de-cf)^5} - \frac{b^2 d^2 f F^{a+\frac{b}{c+dx}} \operatorname{Log}[F]^2}{6(de-cf)^4(e+fx)} + \\ & \frac{b^2 d^3 f F^{a-\frac{bf}{de-cf}} \operatorname{ExpIntegralEi}\left[\frac{bd(e+fx)\operatorname{Log}[F]}{(de-cf)(c+dx)}\right] \operatorname{Log}[F]^2}{(de-cf)^5} - \frac{b^3 d^3 f^2 F^{a-\frac{bf}{de-cf}} \operatorname{ExpIntegralEi}\left[\frac{bd(e+fx)\operatorname{Log}[F]}{(de-cf)(c+dx)}\right] \operatorname{Log}[F]^3}{6(de-cf)^6} \end{aligned}$$

Result (type 8, 23 leaves):

$$\int \frac{F^{a+\frac{b}{c+dx}}}{(e+fx)^4} dx$$

Problem 408: Unable to integrate problem.

$$\int \frac{e^{\frac{e}{c+dx}}}{(a+bx)^3} dx$$

Optimal (type 4, 240 leaves, 18 steps):

$$\begin{aligned} & \frac{d^2 e^{\frac{e}{c+dx}}}{2b(bc-ad)^2} + \frac{d^2 e^{\frac{e}{c+dx}}}{2(bc-ad)^3} - \frac{e^{\frac{e}{c+dx}}}{2b(a+bx)^2} + \frac{de^{\frac{e}{c+dx}}}{2(bc-ad)^2(a+bx)} + \\ & \frac{d^2 e^{\frac{be}{bc-ad}} \operatorname{ExpIntegralEi}\left[-\frac{de(a+bx)}{(bc-ad)(c+dx)}\right]}{(bc-ad)^3} + \frac{bd^2 e^{\frac{be}{bc-ad}} \operatorname{ExpIntegralEi}\left[-\frac{de(a+bx)}{(bc-ad)(c+dx)}\right]}{2(bc-ad)^4} \end{aligned}$$

Result (type 8, 21 leaves):

$$\int \frac{e^{\frac{e}{c+dx}}}{(a+bx)^3} dx$$

Problem 423: Unable to integrate problem.

$$\int \frac{F^{e+\frac{f(a+bx)}{c+dx}}}{(g+hx)^2} dx$$

Optimal (type 4, 159 leaves, 12 steps):

$$\frac{d F^{e+\frac{bf}{d}-\frac{(bc-ad)f}{d(c+dx)}}}{h(dg-ch)} - \frac{F^{e+\frac{f(a+bx)}{c+dx}}}{h(g+hx)} + \frac{(bc-ad) f F^{e+\frac{f(bg-ah)}{dg-ch}} \text{ExpIntegralEi}\left[-\frac{(bc-ad) f (g+hx) \text{Log}[F]}{(dg-ch)(c+dx)}\right] \text{Log}[F]}{(dg-ch)^2}$$

Result (type 8, 28 leaves):

$$\int \frac{F^{e+\frac{f(a+bx)}{c+dx}}}{(g+hx)^2} dx$$

Problem 424: Unable to integrate problem.

$$\int \frac{F^{e+\frac{f(a+bx)}{c+dx}}}{(g+hx)^3} dx$$

Optimal (type 4, 366 leaves, 24 steps):

$$\frac{d^2 F^{e+\frac{bf}{d}-\frac{(bc-ad)f}{d(c+dx)}}}{2h(dg-ch)^2} - \frac{F^{e+\frac{f(a+bx)}{c+dx}}}{2h(g+hx)^2} + \frac{d(bc-ad) f F^{e+\frac{bf}{d}-\frac{(bc-ad)f}{d(c+dx)}} \text{Log}[F]}{2(dg-ch)^3} - \frac{(bc-ad) f F^{e+\frac{f(a+bx)}{c+dx}} \text{Log}[F]}{2(dg-ch)^2(g+hx)} +$$

$$\frac{d(bc-ad) f F^{e+\frac{f(bg-ah)}{dg-ch}} \text{ExpIntegralEi}\left[-\frac{(bc-ad) f (g+hx) \text{Log}[F]}{(dg-ch)(c+dx)}\right] \text{Log}[F]}{(dg-ch)^3} + \frac{(bc-ad)^2 f^2 F^{e+\frac{f(bg-ah)}{dg-ch}} h \text{ExpIntegralEi}\left[-\frac{(bc-ad) f (g+hx) \text{Log}[F]}{(dg-ch)(c+dx)}\right] \text{Log}[F]^2}{2(dg-ch)^4}$$

Result (type 8, 28 leaves):

$$\int \frac{F^{e+\frac{f(a+bx)}{c+dx}}}{(g+hx)^3} dx$$

Problem 425: Unable to integrate problem.

$$\int \frac{F^{e+\frac{f(a+bx)}{c+dx}}}{(g+hx)^4} dx$$

Optimal (type 4, 634 leaves, 48 steps):

$$\frac{d^3 F^{e+\frac{bf}{d}-\frac{(bc-ad)f}{d(c+dx)}}}{3h(dg-ch)^3} - \frac{F^{e+\frac{f(a-bx)}{c+dx}}}{3h(g+hx)^3} + \frac{5d^2(bc-ad)fF^{e+\frac{bf}{d}-\frac{(bc-ad)f}{d(c+dx)}}\text{Log}[F]}{6(dg-ch)^4} - \frac{(bc-ad)fF^{e+\frac{f(a-bx)}{c+dx}}\text{Log}[F]}{6(dg-ch)^2(g+hx)^2} - \frac{2d(bc-ad)fF^{e+\frac{f(a-bx)}{c+dx}}\text{Log}[F]}{3(dg-ch)^3(g+hx)} +$$

$$\frac{d^2(bc-ad)fF^{e+\frac{f(bg-ah)}{dg-ch}}\text{ExpIntegralEi}\left[-\frac{(bc-ad)f(g+hx)\text{Log}[F]}{(dg-ch)(c+dx)}\right]\text{Log}[F]}{(dg-ch)^4} + \frac{d(bc-ad)^2f^2F^{e+\frac{bf}{d}-\frac{(bc-ad)f}{d(c+dx)}}h\text{Log}[F]^2}{6(dg-ch)^5} -$$

$$\frac{(bc-ad)^2f^2F^{e+\frac{f(a-bx)}{c+dx}}h\text{Log}[F]^2}{6(dg-ch)^4(g+hx)} + \frac{d(bc-ad)^2f^2F^{e+\frac{f(bg-ah)}{dg-ch}}h\text{ExpIntegralEi}\left[-\frac{(bc-ad)f(g+hx)\text{Log}[F]}{(dg-ch)(c+dx)}\right]\text{Log}[F]^2}{(dg-ch)^5} +$$

$$\frac{(bc-ad)^3f^3F^{e+\frac{f(bg-ah)}{dg-ch}}h^2\text{ExpIntegralEi}\left[-\frac{(bc-ad)f(g+hx)\text{Log}[F]}{(dg-ch)(c+dx)}\right]\text{Log}[F]^3}{6(dg-ch)^6}$$

Result (type 8, 28 leaves):

$$\int \frac{F^{e+\frac{f(a-bx)}{c+dx}}}{(g+hx)^4} dx$$

Problem 462: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{e^{a+bx}}{x^2(c+dx^2)} dx$$

Optimal (type 4, 145 leaves, 8 steps):

$$-\frac{e^{a+bx}}{cx} + \frac{be^a\text{ExpIntegralEi}[bx]}{c} + \frac{\sqrt{d}e^{a+\frac{b\sqrt{-c}}{\sqrt{d}}}\text{ExpIntegralEi}\left[-\frac{b(\sqrt{-c}-\sqrt{d}x)}{\sqrt{d}}\right]}{2(-c)^{3/2}} - \frac{\sqrt{d}e^{a-\frac{b\sqrt{-c}}{\sqrt{d}}}\text{ExpIntegralEi}\left[\frac{b(\sqrt{-c}+\sqrt{d}x)}{\sqrt{d}}\right]}{2(-c)^{3/2}}$$

Result (type 4, 133 leaves):

$$\frac{1}{2c^{3/2}x} e^a \left(-2\sqrt{c}e^{bx} + 2b\sqrt{c}x\text{ExpIntegralEi}[bx] + i\sqrt{d}e^{\frac{ib\sqrt{c}}{\sqrt{d}}}x\text{ExpIntegralEi}\left[b\left(-\frac{i\sqrt{c}}{\sqrt{d}}+x\right)\right] - i\sqrt{d}e^{-\frac{ib\sqrt{c}}{\sqrt{d}}}x\text{ExpIntegralEi}\left[b\left(\frac{i\sqrt{c}}{\sqrt{d}}+x\right)\right] \right)$$

Problem 463: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{e^{a+bx}}{x(c+dx^2)} dx$$

Optimal (type 4, 111 leaves, 7 steps):

$$\frac{e^a \operatorname{ExpIntegralEi}[bx]}{c} - \frac{e^{a+\frac{b\sqrt{-c}}{\sqrt{d}}} \operatorname{ExpIntegralEi}\left[-\frac{b(\sqrt{-c}-\sqrt{d}x)}{\sqrt{d}}\right]}{2c} - \frac{e^{a-\frac{b\sqrt{-c}}{\sqrt{d}}} \operatorname{ExpIntegralEi}\left[\frac{b(\sqrt{-c}+\sqrt{d}x)}{\sqrt{d}}\right]}{2c}$$

Result (type 4, 93 leaves):

$$\frac{1}{2c} e^a \left(2 \operatorname{ExpIntegralEi}[bx] - e^{-\frac{ib\sqrt{c}}{\sqrt{d}}} \left(e^{\frac{2ib\sqrt{c}}{\sqrt{d}}} \operatorname{ExpIntegralEi}\left[b\left(-\frac{i\sqrt{c}}{\sqrt{d}}+x\right)\right] + \operatorname{ExpIntegralEi}\left[b\left(\frac{i\sqrt{c}}{\sqrt{d}}+x\right)\right] \right) \right)$$

Problem 464: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{e^{a+bx}}{c+dx^2} dx$$

Optimal (type 4, 118 leaves, 4 steps):

$$\frac{e^{a+\frac{b\sqrt{-c}}{\sqrt{d}}} \operatorname{ExpIntegralEi}\left[-\frac{b(\sqrt{-c}-\sqrt{d}x)}{\sqrt{d}}\right]}{2\sqrt{-c}\sqrt{d}} - \frac{e^{a-\frac{b\sqrt{-c}}{\sqrt{d}}} \operatorname{ExpIntegralEi}\left[\frac{b(\sqrt{-c}+\sqrt{d}x)}{\sqrt{d}}\right]}{2\sqrt{-c}\sqrt{d}}$$

Result (type 4, 94 leaves):

$$\frac{i e^{a-\frac{ib\sqrt{c}}{\sqrt{d}}} \left(e^{\frac{2ib\sqrt{c}}{\sqrt{d}}} \operatorname{ExpIntegralEi}\left[b\left(-\frac{i\sqrt{c}}{\sqrt{d}}+x\right)\right] - \operatorname{ExpIntegralEi}\left[b\left(\frac{i\sqrt{c}}{\sqrt{d}}+x\right)\right] \right)}{2\sqrt{c}\sqrt{d}}$$

Problem 465: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{e^{a+bx}}{c+dx^2} dx$$

Optimal (type 4, 100 leaves, 4 steps):

$$\frac{e^{\frac{a+b\sqrt{-c}}{\sqrt{d}}} \text{ExpIntegralEi}\left[-\frac{b(\sqrt{-c}-\sqrt{d}x)}{\sqrt{d}}\right]}{2d} + \frac{e^{\frac{a-b\sqrt{-c}}{\sqrt{d}}} \text{ExpIntegralEi}\left[\frac{b(\sqrt{-c}+\sqrt{d}x)}{\sqrt{d}}\right]}{2d}$$

Result (type 4, 83 leaves):

$$\frac{e^{\frac{a-b\sqrt{-c}}{\sqrt{d}}} \left(e^{\frac{2ib\sqrt{-c}}{\sqrt{d}}} \text{ExpIntegralEi}\left[b\left(-\frac{i\sqrt{c}}{\sqrt{d}}+x\right)\right] + \text{ExpIntegralEi}\left[b\left(\frac{i\sqrt{c}}{\sqrt{d}}+x\right)\right] \right)}{2d}$$

Problem 466: Result unnecessarily involves imaginary or complex numbers.

$$\int \frac{e^{a+bx^2}}{c+dx^2} dx$$

Optimal (type 4, 132 leaves, 7 steps):

$$\frac{e^{a+bx}}{bd} + \frac{\sqrt{-c} e^{\frac{a+b\sqrt{-c}}{\sqrt{d}}} \text{ExpIntegralEi}\left[-\frac{b(\sqrt{-c}-\sqrt{d}x)}{\sqrt{d}}\right]}{2d^{3/2}} - \frac{\sqrt{-c} e^{\frac{a-b\sqrt{-c}}{\sqrt{d}}} \text{ExpIntegralEi}\left[\frac{b(\sqrt{-c}+\sqrt{d}x)}{\sqrt{d}}\right]}{2d^{3/2}}$$

Result (type 4, 120 leaves):

$$\frac{1}{2bd^{3/2}} e^a \left(2\sqrt{d} e^{bx} + ib\sqrt{c} e^{\frac{ib\sqrt{c}}{\sqrt{d}}} \text{ExpIntegralEi}\left[b\left(-\frac{i\sqrt{c}}{\sqrt{d}}+x\right)\right] - ib\sqrt{c} e^{-\frac{ib\sqrt{c}}{\sqrt{d}}} \text{ExpIntegralEi}\left[b\left(\frac{i\sqrt{c}}{\sqrt{d}}+x\right)\right] \right)$$

Problem 485: Result unnecessarily involves higher level functions.

$$\int \frac{2^x}{a+4^{-x}b} dx$$

Optimal (type 3, 43 leaves, 4 steps):

$$\frac{2^x}{a \text{Log}[2]} - \frac{\sqrt{b} \text{ArcTan}\left[\frac{2^x \sqrt{a}}{\sqrt{b}}\right]}{a^{3/2} \text{Log}[2]}$$

Result (type 5, 36 leaves):

$$\frac{8^x \text{Hypergeometric2F1}\left[1, \frac{\text{Log}[8]}{\text{Log}[4]}, \frac{\text{Log}[32]}{\text{Log}[4]}, -\frac{4^x a}{b}\right]}{b \text{Log}[8]}$$

Problem 486: Result unnecessarily involves higher level functions.

$$\int \frac{2^x}{a + 2^{-2x} b} dx$$

Optimal (type 3, 43 leaves, 4 steps):

$$\frac{2^x}{a \operatorname{Log}[2]} - \frac{\sqrt{b} \operatorname{ArcTan}\left[\frac{2^x \sqrt{a}}{\sqrt{b}}\right]}{a^{3/2} \operatorname{Log}[2]}$$

Result (type 5, 36 leaves):

$$\frac{8^x \operatorname{Hypergeometric2F1}\left[1, \frac{\operatorname{Log}[8]}{\operatorname{Log}[4]}, \frac{\operatorname{Log}[32]}{\operatorname{Log}[4]}, -\frac{4^x a}{b}\right]}{b \operatorname{Log}[8]}$$

Problem 487: Result unnecessarily involves higher level functions.

$$\int \frac{2^x}{a - 4^{-x} b} dx$$

Optimal (type 3, 43 leaves, 4 steps):

$$\frac{2^x}{a \operatorname{Log}[2]} - \frac{\sqrt{b} \operatorname{ArcTanh}\left[\frac{2^x \sqrt{a}}{\sqrt{b}}\right]}{a^{3/2} \operatorname{Log}[2]}$$

Result (type 5, 36 leaves):

$$\frac{8^x \operatorname{Hypergeometric2F1}\left[1, \frac{\operatorname{Log}[8]}{\operatorname{Log}[4]}, \frac{\operatorname{Log}[32]}{\operatorname{Log}[4]}, \frac{4^x a}{b}\right]}{b \operatorname{Log}[8]}$$

Problem 488: Result unnecessarily involves higher level functions.

$$\int \frac{2^x}{a - 2^{-2x} b} dx$$

Optimal (type 3, 43 leaves, 4 steps):

$$\frac{2^x}{a \operatorname{Log}[2]} - \frac{\sqrt{b} \operatorname{ArcTanh}\left[\frac{2^x \sqrt{a}}{\sqrt{b}}\right]}{a^{3/2} \operatorname{Log}[2]}$$

Result (type 5, 36 leaves):

$$\frac{8^x \text{Hypergeometric2F1}\left[1, \frac{\text{Log}[8]}{\text{Log}[4]}, \frac{\text{Log}[32]}{\text{Log}[4]}, \frac{4^x a}{b}\right]}{b \text{Log}[8]}$$

Problem 524: Attempted integration timed out after 120 seconds.

$$\int \frac{x}{a + b f^{c+dx} + c f^{2c+2dx}} dx$$

Optimal (type 4, 338 leaves, 9 steps):

$$\begin{aligned} & -\frac{c x^2}{b^2 - 4 a c - b \sqrt{b^2 - 4 a c}} - \frac{c x^2}{b^2 - 4 a c + b \sqrt{b^2 - 4 a c}} - \frac{2 c x \text{Log}\left[1 + \frac{2 c f^{c+dx}}{b - \sqrt{b^2 - 4 a c}}\right]}{\sqrt{b^2 - 4 a c} (b - \sqrt{b^2 - 4 a c}) d \text{Log}[f]} + \\ & \frac{2 c x \text{Log}\left[1 + \frac{2 c f^{c+dx}}{b + \sqrt{b^2 - 4 a c}}\right]}{\sqrt{b^2 - 4 a c} (b + \sqrt{b^2 - 4 a c}) d \text{Log}[f]} - \frac{2 c \text{PolyLog}\left[2, -\frac{2 c f^{c+dx}}{b - \sqrt{b^2 - 4 a c}}\right]}{\sqrt{b^2 - 4 a c} (b - \sqrt{b^2 - 4 a c}) d^2 \text{Log}[f]^2} + \frac{2 c \text{PolyLog}\left[2, -\frac{2 c f^{c+dx}}{b + \sqrt{b^2 - 4 a c}}\right]}{\sqrt{b^2 - 4 a c} (b + \sqrt{b^2 - 4 a c}) d^2 \text{Log}[f]^2} \end{aligned}$$

Result (type 1, 1 leaves):

???

Problem 526: Unable to integrate problem.

$$\int \frac{x^2}{a + b f^{c+dx} + c f^{2c+2dx}} dx$$

Optimal (type 4, 484 leaves, 11 steps):

$$\begin{aligned} & -\frac{2 c x^3}{3 (b^2 - 4 a c - b \sqrt{b^2 - 4 a c})} - \frac{2 c x^3}{3 (b^2 - 4 a c + b \sqrt{b^2 - 4 a c})} - \frac{2 c x^2 \text{Log}\left[1 + \frac{2 c f^{c+dx}}{b - \sqrt{b^2 - 4 a c}}\right]}{\sqrt{b^2 - 4 a c} (b - \sqrt{b^2 - 4 a c}) d \text{Log}[f]} + \\ & \frac{2 c x^2 \text{Log}\left[1 + \frac{2 c f^{c+dx}}{b + \sqrt{b^2 - 4 a c}}\right]}{\sqrt{b^2 - 4 a c} (b + \sqrt{b^2 - 4 a c}) d \text{Log}[f]} - \frac{4 c x \text{PolyLog}\left[2, -\frac{2 c f^{c+dx}}{b - \sqrt{b^2 - 4 a c}}\right]}{\sqrt{b^2 - 4 a c} (b - \sqrt{b^2 - 4 a c}) d^2 \text{Log}[f]^2} + \\ & \frac{4 c x \text{PolyLog}\left[2, -\frac{2 c f^{c+dx}}{b + \sqrt{b^2 - 4 a c}}\right]}{\sqrt{b^2 - 4 a c} (b + \sqrt{b^2 - 4 a c}) d^2 \text{Log}[f]^2} + \frac{4 c \text{PolyLog}\left[3, -\frac{2 c f^{c+dx}}{b - \sqrt{b^2 - 4 a c}}\right]}{\sqrt{b^2 - 4 a c} (b - \sqrt{b^2 - 4 a c}) d^3 \text{Log}[f]^3} - \frac{4 c \text{PolyLog}\left[3, -\frac{2 c f^{c+dx}}{b + \sqrt{b^2 - 4 a c}}\right]}{\sqrt{b^2 - 4 a c} (b + \sqrt{b^2 - 4 a c}) d^3 \text{Log}[f]^3} \end{aligned}$$

Result (type 8, 31 leaves):

$$\int \frac{x^2}{a + b f^{c+dx} + c f^{2c+2dx}} dx$$

Problem 541: Unable to integrate problem.

$$\int \frac{x}{a + b f^{-c-dx} + c f^{c+dx}} dx$$

Optimal (type 4, 203 leaves, 8 steps):

$$\frac{x \operatorname{Log}\left[1 + \frac{2c f^{c+dx}}{a - \sqrt{a^2 - 4bc}}\right]}{\sqrt{a^2 - 4bc} d \operatorname{Log}[f]} - \frac{x \operatorname{Log}\left[1 + \frac{2c f^{c+dx}}{a + \sqrt{a^2 - 4bc}}\right]}{\sqrt{a^2 - 4bc} d \operatorname{Log}[f]} + \frac{\operatorname{PolyLog}\left[2, -\frac{2c f^{c+dx}}{a - \sqrt{a^2 - 4bc}}\right]}{\sqrt{a^2 - 4bc} d^2 \operatorname{Log}[f]^2} - \frac{\operatorname{PolyLog}\left[2, -\frac{2c f^{c+dx}}{a + \sqrt{a^2 - 4bc}}\right]}{\sqrt{a^2 - 4bc} d^2 \operatorname{Log}[f]^2}$$

Result (type 8, 29 leaves):

$$\int \frac{x}{a + b f^{-c-dx} + c f^{c+dx}} dx$$

Problem 542: Unable to integrate problem.

$$\int \frac{x^2}{a + b f^{-c-dx} + c f^{c+dx}} dx$$

Optimal (type 4, 310 leaves, 10 steps):

$$\frac{x^2 \operatorname{Log}\left[1 + \frac{2c f^{c+dx}}{a - \sqrt{a^2 - 4bc}}\right]}{\sqrt{a^2 - 4bc} d \operatorname{Log}[f]} - \frac{x^2 \operatorname{Log}\left[1 + \frac{2c f^{c+dx}}{a + \sqrt{a^2 - 4bc}}\right]}{\sqrt{a^2 - 4bc} d \operatorname{Log}[f]} + \frac{2x \operatorname{PolyLog}\left[2, -\frac{2c f^{c+dx}}{a - \sqrt{a^2 - 4bc}}\right]}{\sqrt{a^2 - 4bc} d^2 \operatorname{Log}[f]^2} - \frac{2x \operatorname{PolyLog}\left[2, -\frac{2c f^{c+dx}}{a + \sqrt{a^2 - 4bc}}\right]}{\sqrt{a^2 - 4bc} d^2 \operatorname{Log}[f]^2} - \frac{2 \operatorname{PolyLog}\left[3, -\frac{2c f^{c+dx}}{a - \sqrt{a^2 - 4bc}}\right]}{\sqrt{a^2 - 4bc} d^3 \operatorname{Log}[f]^3} + \frac{2 \operatorname{PolyLog}\left[3, -\frac{2c f^{c+dx}}{a + \sqrt{a^2 - 4bc}}\right]}{\sqrt{a^2 - 4bc} d^3 \operatorname{Log}[f]^3}$$

Result (type 8, 31 leaves):

$$\int \frac{x^2}{a + b f^{-c-dx} + c f^{c+dx}} dx$$

Problem 544: Unable to integrate problem.

$$\int \frac{\left(a + b F \frac{c\sqrt{d+ex}}{\sqrt{f+gx}} \right)^3}{d f + (e f + d g) x + e g x^2} dx$$

Optimal (type 4, 154 leaves, 6 steps):

$$\frac{6 a^2 b \operatorname{ExpIntegralEi} \left[\frac{c\sqrt{d+ex} \operatorname{Log}[F]}{\sqrt{f+gx}} \right]}{e f - d g} + \frac{6 a b^2 \operatorname{ExpIntegralEi} \left[\frac{2 c\sqrt{d+ex} \operatorname{Log}[F]}{\sqrt{f+gx}} \right]}{e f - d g} + \frac{2 b^3 \operatorname{ExpIntegralEi} \left[\frac{3 c\sqrt{d+ex} \operatorname{Log}[F]}{\sqrt{f+gx}} \right]}{e f - d g} + \frac{2 a^3 \operatorname{Log} \left[\frac{\sqrt{d+ex}}{\sqrt{f+gx}} \right]}{e f - d g}$$

Result (type 8, 52 leaves):

$$\int \frac{\left(a + b F \frac{c\sqrt{d+ex}}{\sqrt{f+gx}} \right)^3}{d f + (e f + d g) x + e g x^2} dx$$

Problem 545: Unable to integrate problem.

$$\int \frac{\left(a + b F \frac{c\sqrt{d+ex}}{\sqrt{f+gx}} \right)^2}{d f + (e f + d g) x + e g x^2} dx$$

Optimal (type 4, 112 leaves, 5 steps):

$$\frac{4 a b \operatorname{ExpIntegralEi} \left[\frac{c\sqrt{d+ex} \operatorname{Log}[F]}{\sqrt{f+gx}} \right]}{e f - d g} + \frac{2 b^2 \operatorname{ExpIntegralEi} \left[\frac{2 c\sqrt{d+ex} \operatorname{Log}[F]}{\sqrt{f+gx}} \right]}{e f - d g} + \frac{2 a^2 \operatorname{Log} \left[\frac{\sqrt{d+ex}}{\sqrt{f+gx}} \right]}{e f - d g}$$

Result (type 8, 52 leaves):

$$\int \frac{\left(a + b F \frac{c\sqrt{d+ex}}{\sqrt{f+gx}} \right)^2}{d f + (e f + d g) x + e g x^2} dx$$

Problem 546: Unable to integrate problem.

$$\int \frac{a + b F^{\frac{c\sqrt{d+ex}}{\sqrt{f+gx}}}}{d f + (e f + d g) x + e g x^2} dx$$

Optimal (type 4, 70 leaves, 4 steps):

$$\frac{2 b \operatorname{ExpIntegralEi}\left[\frac{c\sqrt{d+ex} \operatorname{Log}[F]}{\sqrt{f+gx}}\right]}{e f - d g} + \frac{2 a \operatorname{Log}\left[\frac{\sqrt{d+ex}}{\sqrt{f+gx}}\right]}{e f - d g}$$

Result (type 8, 50 leaves):

$$\int \frac{a + b F^{\frac{c\sqrt{d+ex}}{\sqrt{f+gx}}}}{d f + (e f + d g) x + e g x^2} dx$$

Problem 551: Unable to integrate problem.

$$\int \frac{\left(a + b F^{\frac{c\sqrt{d+ex}}{\sqrt{df-efx}}}\right)^3}{d^2 - e^2 x^2} dx$$

Optimal (type 4, 152 leaves, 6 steps):

$$\frac{3 a^2 b \operatorname{ExpIntegralEi}\left[\frac{c\sqrt{d+ex} \operatorname{Log}[F]}{\sqrt{df-efx}}\right]}{d e} + \frac{3 a b^2 \operatorname{ExpIntegralEi}\left[\frac{2 c\sqrt{d+ex} \operatorname{Log}[F]}{\sqrt{df-efx}}\right]}{d e} + \frac{b^3 \operatorname{ExpIntegralEi}\left[\frac{3 c\sqrt{d+ex} \operatorname{Log}[F]}{\sqrt{df-efx}}\right]}{d e} + \frac{a^3 \operatorname{Log}\left[\frac{\sqrt{d+ex}}{\sqrt{df-efx}}\right]}{d e}$$

Result (type 8, 49 leaves):

$$\int \frac{\left(a + b F^{\frac{c\sqrt{d+ex}}{\sqrt{df-efx}}}\right)^3}{d^2 - e^2 x^2} dx$$

Problem 552: Unable to integrate problem.

$$\int \frac{\left(a + b F \frac{c\sqrt{d+ex}}{\sqrt{df-efx}} \right)^2}{d^2 - e^2 x^2} dx$$

Optimal (type 4, 110 leaves, 5 steps):

$$\frac{2 a b \text{ExpIntegralEi} \left[\frac{c\sqrt{d+ex} \text{Log}[F]}{\sqrt{df-efx}} \right]}{d e} + \frac{b^2 \text{ExpIntegralEi} \left[\frac{2 c\sqrt{d+ex} \text{Log}[F]}{\sqrt{df-efx}} \right]}{d e} + \frac{a^2 \text{Log} \left[\frac{\sqrt{d+ex}}{\sqrt{df-efx}} \right]}{d e}$$

Result (type 8, 49 leaves):

$$\int \frac{\left(a + b F \frac{c\sqrt{d+ex}}{\sqrt{df-efx}} \right)^2}{d^2 - e^2 x^2} dx$$

Problem 553: Unable to integrate problem.

$$\int \frac{a + b F \frac{c\sqrt{d+ex}}{\sqrt{df-efx}}}{d^2 - e^2 x^2} dx$$

Optimal (type 4, 68 leaves, 4 steps):

$$\frac{b \text{ExpIntegralEi} \left[\frac{c\sqrt{d+ex} \text{Log}[F]}{\sqrt{df-efx}} \right]}{d e} + \frac{a \text{Log} \left[\frac{\sqrt{d+ex}}{\sqrt{df-efx}} \right]}{d e}$$

Result (type 8, 47 leaves):

$$\int \frac{a + b F \frac{c\sqrt{d+ex}}{\sqrt{df-efx}}}{d^2 - e^2 x^2} dx$$

Problem 567: Unable to integrate problem.

$$\int \frac{a^x b^x}{x^2} dx$$

Optimal (type 4, 26 leaves, 3 steps):

$$-\frac{a^x b^x}{x} + \text{ExpIntegralEi}\left[x \left(\text{Log}[a] + \text{Log}[b]\right)\right] \left(\text{Log}[a] + \text{Log}[b]\right)$$

Result (type 8, 12 leaves):

$$\int \frac{a^x b^x}{x^2} dx$$

Problem 568: Unable to integrate problem.

$$\int \frac{a^x b^x}{x^3} dx$$

Optimal (type 4, 51 leaves, 4 steps):

$$-\frac{a^x b^x}{2 x^2} - \frac{a^x b^x \left(\text{Log}[a] + \text{Log}[b]\right)}{2 x} + \frac{1}{2} \text{ExpIntegralEi}\left[x \left(\text{Log}[a] + \text{Log}[b]\right)\right] \left(\text{Log}[a] + \text{Log}[b]\right)^2$$

Result (type 8, 12 leaves):

$$\int \frac{a^x b^x}{x^3} dx$$

Problem 572: Result more than twice size of optimal antiderivative.

$$\int \frac{(d + e e^{h+ix}) (f + g x)^3}{a + b e^{h+ix} + c e^{2h+2ix}} dx$$

Optimal (type 4, 770 leaves, 13 steps):

$$\begin{aligned}
& \frac{\left(e - \frac{2cd-be}{\sqrt{b^2-4ac}}\right) (f+gx)^4}{4(b+\sqrt{b^2-4ac})g} + \frac{\left(e + \frac{2cd-be}{\sqrt{b^2-4ac}}\right) (f+gx)^4}{4(b-\sqrt{b^2-4ac})g} - \frac{\left(e + \frac{2cd-be}{\sqrt{b^2-4ac}}\right) (f+gx)^3 \operatorname{Log}\left[1 + \frac{2ce^{h+ix}}{b-\sqrt{b^2-4ac}}\right]}{(b-\sqrt{b^2-4ac})i} \\
& \frac{\left(e - \frac{2cd-be}{\sqrt{b^2-4ac}}\right) (f+gx)^3 \operatorname{Log}\left[1 + \frac{2ce^{h+ix}}{b+\sqrt{b^2-4ac}}\right]}{(b+\sqrt{b^2-4ac})i} - \frac{3\left(e + \frac{2cd-be}{\sqrt{b^2-4ac}}\right) g (f+gx)^2 \operatorname{PolyLog}\left[2, -\frac{2ce^{h+ix}}{b-\sqrt{b^2-4ac}}\right]}{(b-\sqrt{b^2-4ac})i^2} \\
& \frac{3\left(e - \frac{2cd-be}{\sqrt{b^2-4ac}}\right) g (f+gx)^2 \operatorname{PolyLog}\left[2, -\frac{2ce^{h+ix}}{b+\sqrt{b^2-4ac}}\right]}{(b+\sqrt{b^2-4ac})i^2} + \frac{6\left(e + \frac{2cd-be}{\sqrt{b^2-4ac}}\right) g^2 (f+gx) \operatorname{PolyLog}\left[3, -\frac{2ce^{h+ix}}{b-\sqrt{b^2-4ac}}\right]}{(b-\sqrt{b^2-4ac})i^3} \\
& \frac{6\left(e - \frac{2cd-be}{\sqrt{b^2-4ac}}\right) g^2 (f+gx) \operatorname{PolyLog}\left[3, -\frac{2ce^{h+ix}}{b+\sqrt{b^2-4ac}}\right]}{(b+\sqrt{b^2-4ac})i^3} - \frac{6\left(e + \frac{2cd-be}{\sqrt{b^2-4ac}}\right) g^3 \operatorname{PolyLog}\left[4, -\frac{2ce^{h+ix}}{b-\sqrt{b^2-4ac}}\right]}{(b-\sqrt{b^2-4ac})i^4} - \frac{6\left(e - \frac{2cd-be}{\sqrt{b^2-4ac}}\right) g^3 \operatorname{PolyLog}\left[4, -\frac{2ce^{h+ix}}{b+\sqrt{b^2-4ac}}\right]}{(b+\sqrt{b^2-4ac})i^4}
\end{aligned}$$

Result (type 4, 3479 leaves):

$$\begin{aligned}
& \frac{2e f^3 \operatorname{ArcTan}\left[\frac{b+2ce^{h+ix}}{\sqrt{-b^2+4ac}}\right]}{\sqrt{-b^2+4ac}i} - \frac{d f^3 \left(-2x + \frac{2b \operatorname{ArcTan}\left[\frac{b+2ce^{h+ix}}{\sqrt{-b^2+4ac}}\right]}{\sqrt{-b^2+4ac}i} + \frac{\operatorname{Log}\left[a+e^{h+ix}(b+ce^{h+ix})\right]}{i}\right)}{2a} + \\
& 3df^2g \left(\frac{2e^{-h} \left(\frac{x^2}{2(b-\sqrt{b^2-4ac})} - \frac{x \operatorname{Log}\left[1 + \frac{2ce^{h+ix}}{b-\sqrt{b^2-4ac}}\right]}{(b-\sqrt{b^2-4ac})i} - \frac{\operatorname{PolyLog}\left[2, -\frac{2ce^{h+ix}}{b-\sqrt{b^2-4ac}}\right]}{(b-\sqrt{b^2-4ac})i^2} \right)}{\frac{-be^{-h-\sqrt{b^2-4ac}}e^{-h}}{2c} - \frac{-be^{-h+\sqrt{b^2-4ac}}e^{-h}}{2c}} + \frac{2e^{-h} \left(\frac{x^2}{2(b+\sqrt{b^2-4ac})} - \frac{x \operatorname{Log}\left[1 + \frac{2ce^{h+ix}}{b+\sqrt{b^2-4ac}}\right]}{(b+\sqrt{b^2-4ac})i} - \frac{\operatorname{PolyLog}\left[2, -\frac{2ce^{h+ix}}{b+\sqrt{b^2-4ac}}\right]}{(b+\sqrt{b^2-4ac})i^2} \right)}{\frac{-be^{-h-\sqrt{b^2-4ac}}e^{-h}}{2c} - \frac{-be^{-h+\sqrt{b^2-4ac}}e^{-h}}{2c}} \right) + \\
& 3ef^2g \left(\frac{\left(-be^{-h} + \sqrt{b^2-4ac}\right)e^{-h} \left(\frac{x^2}{2(b-\sqrt{b^2-4ac})} - \frac{x \operatorname{Log}\left[1 + \frac{2ce^{h+ix}}{b-\sqrt{b^2-4ac}}\right]}{(b-\sqrt{b^2-4ac})i} - \frac{\operatorname{PolyLog}\left[2, -\frac{2ce^{h+ix}}{b-\sqrt{b^2-4ac}}\right]}{(b-\sqrt{b^2-4ac})i^2} \right)}{c \left(\frac{-be^{-h-\sqrt{b^2-4ac}}e^{-h}}{2c} - \frac{-be^{-h+\sqrt{b^2-4ac}}e^{-h}}{2c} \right)} \right) +
\end{aligned}$$

$$\begin{aligned}
& \left(\frac{-b e^{-h} - \sqrt{b^2 - 4ac} e^{-h}}{2c} \left(\frac{x^2}{2(b + \sqrt{b^2 - 4ac})} - \frac{x \operatorname{Log}\left[1 + \frac{2c e^{h+ix}}{b + \sqrt{b^2 - 4ac}}\right]}{(b + \sqrt{b^2 - 4ac})i} - \frac{\operatorname{PolyLog}\left[2, -\frac{2c e^{h+ix}}{b + \sqrt{b^2 - 4ac}}\right]}{(b + \sqrt{b^2 - 4ac})i^2} \right) \right) + \\
& \left(\frac{-b e^{-h} - \sqrt{b^2 - 4ac} e^{-h}}{2c} - \frac{-b e^{-h} + \sqrt{b^2 - 4ac} e^{-h}}{2c} \right) + \\
& 3dfg^2 \left(\frac{2e^{-h} \left(\frac{x^3}{3(b - \sqrt{b^2 - 4ac})} - \frac{x^2 \operatorname{Log}\left[1 + \frac{2c e^{h+ix}}{b - \sqrt{b^2 - 4ac}}\right]}{(b - \sqrt{b^2 - 4ac})i} - \frac{2x \operatorname{PolyLog}\left[2, -\frac{2c e^{h+ix}}{b - \sqrt{b^2 - 4ac}}\right]}{(b - \sqrt{b^2 - 4ac})i^2} + \frac{2 \operatorname{PolyLog}\left[3, -\frac{2c e^{h+ix}}{b - \sqrt{b^2 - 4ac}}\right]}{(b - \sqrt{b^2 - 4ac})i^3} \right)}{\frac{-b e^{-h} - \sqrt{b^2 - 4ac} e^{-h}}{2c} - \frac{-b e^{-h} + \sqrt{b^2 - 4ac} e^{-h}}{2c}} \right) + \\
& \left(\frac{2e^{-h} \left(\frac{x^3}{3(b + \sqrt{b^2 - 4ac})} - \frac{x^2 \operatorname{Log}\left[1 + \frac{2c e^{h+ix}}{b + \sqrt{b^2 - 4ac}}\right]}{(b + \sqrt{b^2 - 4ac})i} - \frac{2x \operatorname{PolyLog}\left[2, -\frac{2c e^{h+ix}}{b + \sqrt{b^2 - 4ac}}\right]}{(b + \sqrt{b^2 - 4ac})i^2} + \frac{2 \operatorname{PolyLog}\left[3, -\frac{2c e^{h+ix}}{b + \sqrt{b^2 - 4ac}}\right]}{(b + \sqrt{b^2 - 4ac})i^3} \right)}{\frac{-b e^{-h} - \sqrt{b^2 - 4ac} e^{-h}}{2c} - \frac{-b e^{-h} + \sqrt{b^2 - 4ac} e^{-h}}{2c}} \right) + \\
& 3efg^2 \left(\left(\left(\left(-b e^{-h} + \sqrt{b^2 - 4ac} e^{-h} \right) \left(\frac{x^3}{3(b - \sqrt{b^2 - 4ac})} - \frac{x^2 \operatorname{Log}\left[1 + \frac{2c e^{h+ix}}{b - \sqrt{b^2 - 4ac}}\right]}{(b - \sqrt{b^2 - 4ac})i} - \frac{2x \operatorname{PolyLog}\left[2, -\frac{2c e^{h+ix}}{b - \sqrt{b^2 - 4ac}}\right]}{(b - \sqrt{b^2 - 4ac})i^2} + \frac{2 \operatorname{PolyLog}\left[3, -\frac{2c e^{h+ix}}{b - \sqrt{b^2 - 4ac}}\right]}{(b - \sqrt{b^2 - 4ac})i^3} \right) \right) \right) \right) / \\
& \left(c \left(\frac{-b e^{-h} - \sqrt{b^2 - 4ac} e^{-h}}{2c} - \frac{-b e^{-h} + \sqrt{b^2 - 4ac} e^{-h}}{2c} \right) \right) + \\
& \left(\left(\left(-b e^{-h} - \sqrt{b^2 - 4ac} e^{-h} \right) \left(\frac{x^3}{3(b + \sqrt{b^2 - 4ac})} - \frac{x^2 \operatorname{Log}\left[1 + \frac{2c e^{h+ix}}{b + \sqrt{b^2 - 4ac}}\right]}{(b + \sqrt{b^2 - 4ac})i} - \frac{2x \operatorname{PolyLog}\left[2, -\frac{2c e^{h+ix}}{b + \sqrt{b^2 - 4ac}}\right]}{(b + \sqrt{b^2 - 4ac})i^2} + \frac{2 \operatorname{PolyLog}\left[3, -\frac{2c e^{h+ix}}{b + \sqrt{b^2 - 4ac}}\right]}{(b + \sqrt{b^2 - 4ac})i^3} \right) \right) \right) / \\
& \left(c \left(\frac{-b e^{-h} - \sqrt{b^2 - 4ac} e^{-h}}{2c} - \frac{-b e^{-h} + \sqrt{b^2 - 4ac} e^{-h}}{2c} \right) \right) +
\end{aligned}$$

$$\begin{aligned}
& d g^3 \left(- \left(\left(2 e^{-h} \left(\frac{x^4}{4 (b - \sqrt{b^2 - 4 a c})} - \frac{x^3 \operatorname{Log} \left[1 + \frac{2 c e^{h+i x}}{b - \sqrt{b^2 - 4 a c}} \right]}{(b - \sqrt{b^2 - 4 a c}) i} - \frac{3 x^2 \operatorname{PolyLog} \left[2, -\frac{2 c e^{h+i x}}{b - \sqrt{b^2 - 4 a c}} \right]}{(b - \sqrt{b^2 - 4 a c}) i^2} + \frac{6 x \operatorname{PolyLog} \left[3, -\frac{2 c e^{h+i x}}{b - \sqrt{b^2 - 4 a c}} \right]}{(b - \sqrt{b^2 - 4 a c}) i^3} \right. \right. \right. \\
& \left. \left. \left. \frac{6 \operatorname{PolyLog} \left[4, -\frac{2 c e^{h+i x}}{b - \sqrt{b^2 - 4 a c}} \right]}{(b - \sqrt{b^2 - 4 a c}) i^4} \right] \right) \right) / \left(\frac{-b e^{-h} - \sqrt{b^2 - 4 a c} e^{-h}}{2 c} - \frac{-b e^{-h} + \sqrt{b^2 - 4 a c} e^{-h}}{2 c} \right) \right) + \\
& \left(2 e^{-h} \left(\frac{x^4}{4 (b + \sqrt{b^2 - 4 a c})} - \frac{x^3 \operatorname{Log} \left[1 + \frac{2 c e^{h+i x}}{b + \sqrt{b^2 - 4 a c}} \right]}{(b + \sqrt{b^2 - 4 a c}) i} - \frac{3 x^2 \operatorname{PolyLog} \left[2, -\frac{2 c e^{h+i x}}{b + \sqrt{b^2 - 4 a c}} \right]}{(b + \sqrt{b^2 - 4 a c}) i^2} + \frac{6 x \operatorname{PolyLog} \left[3, -\frac{2 c e^{h+i x}}{b + \sqrt{b^2 - 4 a c}} \right]}{(b + \sqrt{b^2 - 4 a c}) i^3} \right. \right. \\
& \left. \left. \left. \frac{6 \operatorname{PolyLog} \left[4, -\frac{2 c e^{h+i x}}{b + \sqrt{b^2 - 4 a c}} \right]}{(b + \sqrt{b^2 - 4 a c}) i^4} \right] \right) \right) / \left(\frac{-b e^{-h} - \sqrt{b^2 - 4 a c} e^{-h}}{2 c} - \frac{-b e^{-h} + \sqrt{b^2 - 4 a c} e^{-h}}{2 c} \right) \right) + \\
& e g^3 \left(- \left(\left(\left(-b e^{-h} + \sqrt{b^2 - 4 a c} e^{-h} \right) \left(\frac{x^4}{4 (b - \sqrt{b^2 - 4 a c})} - \frac{x^3 \operatorname{Log} \left[1 + \frac{2 c e^{h+i x}}{b - \sqrt{b^2 - 4 a c}} \right]}{(b - \sqrt{b^2 - 4 a c}) i} - \frac{3 x^2 \operatorname{PolyLog} \left[2, -\frac{2 c e^{h+i x}}{b - \sqrt{b^2 - 4 a c}} \right]}{(b - \sqrt{b^2 - 4 a c}) i^2} + \right. \right. \right. \\
& \left. \left. \left. \frac{6 x \operatorname{PolyLog} \left[3, -\frac{2 c e^{h+i x}}{b - \sqrt{b^2 - 4 a c}} \right]}{(b - \sqrt{b^2 - 4 a c}) i^3} - \frac{6 \operatorname{PolyLog} \left[4, -\frac{2 c e^{h+i x}}{b - \sqrt{b^2 - 4 a c}} \right]}{(b - \sqrt{b^2 - 4 a c}) i^4} \right] \right) \right) \right) / \left(c \left(\frac{-b e^{-h} - \sqrt{b^2 - 4 a c} e^{-h}}{2 c} - \frac{-b e^{-h} + \sqrt{b^2 - 4 a c} e^{-h}}{2 c} \right) \right) \right) + \\
& \left(\left(-b e^{-h} - \sqrt{b^2 - 4 a c} e^{-h} \right) \left(\frac{x^4}{4 (b + \sqrt{b^2 - 4 a c})} - \frac{x^3 \operatorname{Log} \left[1 + \frac{2 c e^{h+i x}}{b + \sqrt{b^2 - 4 a c}} \right]}{(b + \sqrt{b^2 - 4 a c}) i} - \frac{3 x^2 \operatorname{PolyLog} \left[2, -\frac{2 c e^{h+i x}}{b + \sqrt{b^2 - 4 a c}} \right]}{(b + \sqrt{b^2 - 4 a c}) i^2} + \right. \right. \\
& \left. \left. \left. \frac{6 x \operatorname{PolyLog} \left[3, -\frac{2 c e^{h+i x}}{b + \sqrt{b^2 - 4 a c}} \right]}{(b + \sqrt{b^2 - 4 a c}) i^3} - \frac{6 \operatorname{PolyLog} \left[4, -\frac{2 c e^{h+i x}}{b + \sqrt{b^2 - 4 a c}} \right]}{(b + \sqrt{b^2 - 4 a c}) i^4} \right] \right) \right) \right) / \left(c \left(\frac{-b e^{-h} - \sqrt{b^2 - 4 a c} e^{-h}}{2 c} - \frac{-b e^{-h} + \sqrt{b^2 - 4 a c} e^{-h}}{2 c} \right) \right) \right)
\end{aligned}$$

Problem 573: Result more than twice size of optimal antiderivative.

$$\int \frac{(d + e e^{h+i x}) (f + g x)^2}{a + b e^{h+i x} + c e^{2h+2i x}} dx$$

Optimal (type 4, 599 leaves, 11 steps):

$$\begin{aligned}
 & \frac{\left(e - \frac{2cd-be}{\sqrt{b^2-4ac}}\right) (f+gx)^3}{3(b+\sqrt{b^2-4ac})g} + \frac{\left(e + \frac{2cd-be}{\sqrt{b^2-4ac}}\right) (f+gx)^3}{3(b-\sqrt{b^2-4ac})g} - \frac{\left(e + \frac{2cd-be}{\sqrt{b^2-4ac}}\right) (f+gx)^2 \operatorname{Log}\left[1 + \frac{2ce^{h+ix}}{b-\sqrt{b^2-4ac}}\right]}{(b-\sqrt{b^2-4ac})i} - \\
 & \frac{\left(e - \frac{2cd-be}{\sqrt{b^2-4ac}}\right) (f+gx)^2 \operatorname{Log}\left[1 + \frac{2ce^{h+ix}}{b+\sqrt{b^2-4ac}}\right]}{(b+\sqrt{b^2-4ac})i} - \frac{2\left(e + \frac{2cd-be}{\sqrt{b^2-4ac}}\right) g(f+gx) \operatorname{PolyLog}\left[2, -\frac{2ce^{h+ix}}{b-\sqrt{b^2-4ac}}\right]}{(b-\sqrt{b^2-4ac})i^2} - \\
 & \frac{2\left(e - \frac{2cd-be}{\sqrt{b^2-4ac}}\right) g(f+gx) \operatorname{PolyLog}\left[2, -\frac{2ce^{h+ix}}{b+\sqrt{b^2-4ac}}\right]}{(b+\sqrt{b^2-4ac})i^2} + \frac{2\left(e + \frac{2cd-be}{\sqrt{b^2-4ac}}\right) g^2 \operatorname{PolyLog}\left[3, -\frac{2ce^{h+ix}}{b-\sqrt{b^2-4ac}}\right]}{(b-\sqrt{b^2-4ac})i^3} + \frac{2\left(e - \frac{2cd-be}{\sqrt{b^2-4ac}}\right) g^2 \operatorname{PolyLog}\left[3, -\frac{2ce^{h+ix}}{b+\sqrt{b^2-4ac}}\right]}{(b+\sqrt{b^2-4ac})i^3}
 \end{aligned}$$

Result (type 4, 1412 leaves):

$$\begin{aligned}
& - \frac{1}{6 a \sqrt{-(b^2 - 4 a c)^2} i^3} \\
& \left(-6 \sqrt{-(b^2 - 4 a c)^2} d f^2 i^3 x - 6 \sqrt{-(b^2 - 4 a c)^2} d f g i^3 x^2 - 2 \sqrt{-(b^2 - 4 a c)^2} d g^2 i^3 x^3 + 6 b \sqrt{b^2 - 4 a c} d f^2 i^2 \operatorname{ArcTan}\left[\frac{b + 2 c e^{h+i x}}{\sqrt{-b^2 + 4 a c}}\right] - \right. \\
& 12 a \sqrt{b^2 - 4 a c} e f^2 i^2 \operatorname{ArcTan}\left[\frac{b + 2 c e^{h+i x}}{\sqrt{-b^2 + 4 a c}}\right] + 6 \sqrt{-(b^2 - 4 a c)^2} d f g i^2 x \operatorname{Log}\left[1 + \frac{2 c e^{h+i x}}{b - \sqrt{b^2 - 4 a c}}\right] + \\
& 6 b \sqrt{-b^2 + 4 a c} d f g i^2 x \operatorname{Log}\left[1 + \frac{2 c e^{h+i x}}{b - \sqrt{b^2 - 4 a c}}\right] - 12 a \sqrt{-b^2 + 4 a c} e f g i^2 x \operatorname{Log}\left[1 + \frac{2 c e^{h+i x}}{b - \sqrt{b^2 - 4 a c}}\right] + \\
& 3 \sqrt{-(b^2 - 4 a c)^2} d g^2 i^2 x^2 \operatorname{Log}\left[1 + \frac{2 c e^{h+i x}}{b - \sqrt{b^2 - 4 a c}}\right] + 3 b \sqrt{-b^2 + 4 a c} d g^2 i^2 x^2 \operatorname{Log}\left[1 + \frac{2 c e^{h+i x}}{b - \sqrt{b^2 - 4 a c}}\right] - \\
& 6 a \sqrt{-b^2 + 4 a c} e g^2 i^2 x^2 \operatorname{Log}\left[1 + \frac{2 c e^{h+i x}}{b - \sqrt{b^2 - 4 a c}}\right] + 6 \sqrt{-(b^2 - 4 a c)^2} d f g i^2 x \operatorname{Log}\left[1 + \frac{2 c e^{h+i x}}{b + \sqrt{b^2 - 4 a c}}\right] - \\
& 6 b \sqrt{-b^2 + 4 a c} d f g i^2 x \operatorname{Log}\left[1 + \frac{2 c e^{h+i x}}{b + \sqrt{b^2 - 4 a c}}\right] + 12 a \sqrt{-b^2 + 4 a c} e f g i^2 x \operatorname{Log}\left[1 + \frac{2 c e^{h+i x}}{b + \sqrt{b^2 - 4 a c}}\right] + \\
& 3 \sqrt{-(b^2 - 4 a c)^2} d g^2 i^2 x^2 \operatorname{Log}\left[1 + \frac{2 c e^{h+i x}}{b + \sqrt{b^2 - 4 a c}}\right] - 3 b \sqrt{-b^2 + 4 a c} d g^2 i^2 x^2 \operatorname{Log}\left[1 + \frac{2 c e^{h+i x}}{b + \sqrt{b^2 - 4 a c}}\right] + \\
& 6 a \sqrt{-b^2 + 4 a c} e g^2 i^2 x^2 \operatorname{Log}\left[1 + \frac{2 c e^{h+i x}}{b + \sqrt{b^2 - 4 a c}}\right] + 3 \sqrt{-(b^2 - 4 a c)^2} d f^2 i^2 \operatorname{Log}\left[a + e^{h+i x} (b + c e^{h+i x})\right] + \\
& 6 \left(\sqrt{-(b^2 - 4 a c)^2} d + b \sqrt{-b^2 + 4 a c} d - 2 a \sqrt{-b^2 + 4 a c} e \right) g i (f + g x) \operatorname{PolyLog}\left[2, \frac{2 c e^{h+i x}}{-b + \sqrt{b^2 - 4 a c}}\right] + \\
& 6 \left(\sqrt{-(b^2 - 4 a c)^2} d - b \sqrt{-b^2 + 4 a c} d + 2 a \sqrt{-b^2 + 4 a c} e \right) g i (f + g x) \operatorname{PolyLog}\left[2, -\frac{2 c e^{h+i x}}{b + \sqrt{b^2 - 4 a c}}\right] - \\
& 6 \sqrt{-(b^2 - 4 a c)^2} d g^2 \operatorname{PolyLog}\left[3, \frac{2 c e^{h+i x}}{-b + \sqrt{b^2 - 4 a c}}\right] - 6 b \sqrt{-b^2 + 4 a c} d g^2 \operatorname{PolyLog}\left[3, \frac{2 c e^{h+i x}}{-b + \sqrt{b^2 - 4 a c}}\right] + \\
& 12 a \sqrt{-b^2 + 4 a c} e g^2 \operatorname{PolyLog}\left[3, \frac{2 c e^{h+i x}}{-b + \sqrt{b^2 - 4 a c}}\right] - 6 \sqrt{-(b^2 - 4 a c)^2} d g^2 \operatorname{PolyLog}\left[3, -\frac{2 c e^{h+i x}}{b + \sqrt{b^2 - 4 a c}}\right] + \\
& \left. 6 b \sqrt{-b^2 + 4 a c} d g^2 \operatorname{PolyLog}\left[3, -\frac{2 c e^{h+i x}}{b + \sqrt{b^2 - 4 a c}}\right] - 12 a \sqrt{-b^2 + 4 a c} e g^2 \operatorname{PolyLog}\left[3, -\frac{2 c e^{h+i x}}{b + \sqrt{b^2 - 4 a c}}\right] \right)
\end{aligned}$$

Problem 579: Unable to integrate problem.

$$\int F^{a+b \operatorname{Log}[c+d x^n]} x^2 dx$$

Optimal (type 5, 65 leaves, 4 steps):

$$\frac{1}{3} F^a x^3 (c+d x^n)^{b \operatorname{Log}[F]} \left(1 + \frac{d x^n}{c}\right)^{-b \operatorname{Log}[F]} \operatorname{Hypergeometric2F1}\left[\frac{3}{n}, -b \operatorname{Log}[F], \frac{3+n}{n}, -\frac{d x^n}{c}\right]$$

Result (type 8, 20 leaves):

$$\int F^{a+b \operatorname{Log}[c+d x^n]} x^2 dx$$

Problem 580: Unable to integrate problem.

$$\int F^{a+b \operatorname{Log}[c+d x^n]} x dx$$

Optimal (type 5, 65 leaves, 4 steps):

$$\frac{1}{2} F^a x^2 (c+d x^n)^{b \operatorname{Log}[F]} \left(1 + \frac{d x^n}{c}\right)^{-b \operatorname{Log}[F]} \operatorname{Hypergeometric2F1}\left[\frac{2}{n}, -b \operatorname{Log}[F], \frac{2+n}{n}, -\frac{d x^n}{c}\right]$$

Result (type 8, 18 leaves):

$$\int F^{a+b \operatorname{Log}[c+d x^n]} x dx$$

Problem 581: Unable to integrate problem.

$$\int F^{a+b \operatorname{Log}[c+d x^n]} dx$$

Optimal (type 5, 56 leaves, 4 steps):

$$F^a x (c+d x^n)^{b \operatorname{Log}[F]} \left(1 + \frac{d x^n}{c}\right)^{-b \operatorname{Log}[F]} \operatorname{Hypergeometric2F1}\left[\frac{1}{n}, -b \operatorname{Log}[F], 1 + \frac{1}{n}, -\frac{d x^n}{c}\right]$$

Result (type 8, 16 leaves):

$$\int F^{a+b \operatorname{Log}[c+d x^n]} dx$$

Problem 583: Unable to integrate problem.

$$\int \frac{F^{a+b \operatorname{Log}[c+d x^n]}}{x^2} dx$$

Optimal (type 5, 66 leaves, 4 steps):

$$\frac{F^a (c+d x^n)^{b \operatorname{Log}[F]} \left(1 + \frac{d x^n}{c}\right)^{-b \operatorname{Log}[F]} \operatorname{Hypergeometric2F1}\left[-\frac{1}{n}, -b \operatorname{Log}[F], -\frac{1-n}{n}, -\frac{d x^n}{c}\right]}{x}$$

Result (type 8, 20 leaves):

$$\int \frac{F^{a+b \operatorname{Log}[c+d x^n]}}{x^2} dx$$

Problem 584: Unable to integrate problem.

$$\int \frac{F^{a+b \operatorname{Log}[c+d x^n]}}{x^3} dx$$

Optimal (type 5, 68 leaves, 4 steps):

$$\frac{F^a (c+d x^n)^{b \operatorname{Log}[F]} \left(1 + \frac{d x^n}{c}\right)^{-b \operatorname{Log}[F]} \operatorname{Hypergeometric2F1}\left[-\frac{2}{n}, -b \operatorname{Log}[F], -\frac{2-n}{n}, -\frac{d x^n}{c}\right]}{2 x^2}$$

Result (type 8, 20 leaves):

$$\int \frac{F^{a+b \operatorname{Log}[c+d x^n]}}{x^3} dx$$

Problem 585: Unable to integrate problem.

$$\int F^{a+b \operatorname{Log}[c+d x^n]} (d x)^m dx$$

Optimal (type 5, 77 leaves, 4 steps):

$$\frac{F^a (d x)^{1+m} (c+d x^n)^{b \operatorname{Log}[F]} \left(1 + \frac{d x^n}{c}\right)^{-b \operatorname{Log}[F]} \operatorname{Hypergeometric2F1}\left[\frac{1+m}{n}, -b \operatorname{Log}[F], \frac{1+m+n}{n}, -\frac{d x^n}{c}\right]}{d (1+m)}$$

Result (type 8, 22 leaves):

$$\int F^{a+b \operatorname{Log}[c+d x^n]} (d x)^m dx$$

Problem 586: Unable to integrate problem.

$$\int e^{\text{Log}[(d+ex)^n]^2} (d+ex)^m dx$$

Optimal (type 4, 76 leaves, 3 steps):

$$\frac{e^{-\frac{(1+m)^2}{4n^2}} \sqrt{\pi} (d+ex)^{1+m} ((d+ex)^n)^{-\frac{1+m}{n}} \text{Erfi}\left[\frac{1+m+2n \text{Log}[(d+ex)^n]}{2n}\right]}{2en}$$

Result (type 8, 22 leaves):

$$\int e^{\text{Log}[(d+ex)^n]^2} (d+ex)^m dx$$

Problem 587: Unable to integrate problem.

$$\int F^{f(a+b \text{Log}[c(d+ex)^n]^2)} (dg+egx)^m dx$$

Optimal (type 4, 137 leaves, 3 steps):

$$\frac{e^{-\frac{(1+m)^2}{4bf n^2 \text{Log}[F]}} F^{af} \sqrt{\pi} (c(d+ex)^n)^{-\frac{1+m}{n}} (dg+egx)^{1+m} \text{Erfi}\left[\frac{1+m+2bf n \text{Log}[F] \text{Log}[c(d+ex)^n]}{2\sqrt{b}\sqrt{f} n \sqrt{\text{Log}[F]}}\right]}{2\sqrt{b} e \sqrt{f} g n \sqrt{\text{Log}[F]}}$$

Result (type 8, 33 leaves):

$$\int F^{f(a+b \text{Log}[c(d+ex)^n]^2)} (dg+egx)^m dx$$

Problem 602: Unable to integrate problem.

$$\int F^{f(a+b \text{Log}[c(d+ex)^n]^2)} (dg+egx)^m dx$$

Optimal (type 4, 153 leaves, 4 steps):

$$\frac{1}{2be\sqrt{f} n \sqrt{\text{Log}[F]}} e^{-\frac{(1+m+2abfn \text{Log}[F])^2}{4b^2fn^2 \text{Log}[F]}} F^{a^2f} \sqrt{\pi} (d+ex) (c(d+ex)^n)^{-\frac{1+m}{n}} (dg+egx)^m \text{Erfi}\left[\frac{1+m+2abfn \text{Log}[F] + 2b^2fn \text{Log}[F] \text{Log}[c(d+ex)^n]}{2b\sqrt{f} n \sqrt{\text{Log}[F]}}\right]$$

Result (type 8, 33 leaves):

$$\int F^{f(a+b \text{Log}[c(d+ex)^n]^2)} (dg+egx)^m dx$$

Problem 619: Unable to integrate problem.

$$\int e^{a+bx+cx^2} (b+2cx) (a+bx+cx^2)^m dx$$

Optimal (type 4, 49 leaves, 2 steps):

$$(-a-bx-cx^2)^{-m} (a+bx+cx^2)^m \text{Gamma}[1+m, -a-bx-cx^2]$$

Result (type 8, 33 leaves):

$$\int e^{a+bx+cx^2} (b+2cx) (a+bx+cx^2)^m dx$$

Problem 636: Result more than twice size of optimal antiderivative.

$$\int \frac{e^{-x}}{\sqrt{1-e^{-2x}}} dx$$

Optimal (type 3, 8 leaves, 2 steps):

$$-\text{ArcSin}[e^{-x}]$$

Result (type 3, 42 leaves):

$$\frac{e^{-x} \sqrt{-1+e^{2x}} \text{ArcTan}[\sqrt{-1+e^{2x}}]}{\sqrt{1-e^{-2x}}}$$

Problem 638: Result more than twice size of optimal antiderivative.

$$\int \frac{e^x}{1-e^{2x}} dx$$

Optimal (type 3, 4 leaves, 2 steps):

$$\text{ArcTanh}[e^x]$$

Result (type 3, 23 leaves):

$$-\frac{1}{2} \text{Log}[1-e^x] + \frac{1}{2} \text{Log}[1+e^x]$$

Problem 652: Result more than twice size of optimal antiderivative.

$$\int \frac{e^x}{-1 + e^{2x}} dx$$

Optimal (type 3, 6 leaves, 2 steps):

$$-\text{ArcTanh}[e^x]$$

Result (type 3, 23 leaves):

$$\frac{1}{2} \text{Log}[1 - e^x] - \frac{1}{2} \text{Log}[1 + e^x]$$

Problem 681: Result more than twice size of optimal antiderivative.

$$\int e^x \text{Sech}[e^x] dx$$

Optimal (type 3, 5 leaves, 2 steps):

$$\text{ArcTan}[\text{Sinh}[e^x]]$$

Result (type 3, 11 leaves):

$$2 \text{ArcTan}\left[\text{Tanh}\left[\frac{e^x}{2}\right]\right]$$

Problem 684: Result more than twice size of optimal antiderivative.

$$\int e^x \text{Sec}[1 - e^x]^3 dx$$

Optimal (type 3, 34 leaves, 3 steps):

$$-\frac{1}{2} \text{ArcTanh}[\text{Sin}[1 - e^x]] - \frac{1}{2} \text{Sec}[1 - e^x] \text{Tan}[1 - e^x]$$

Result (type 3, 79 leaves):

$$\frac{1}{2} \left(\text{Log}\left[\text{Cos}\left[\frac{1}{2}(1 - e^x)\right]\right] - \text{Sin}\left[\frac{1}{2}(1 - e^x)\right] \right) - \text{Log}\left[\text{Cos}\left[\frac{1}{2}(1 - e^x)\right] + \text{Sin}\left[\frac{1}{2}(1 - e^x)\right]\right] - \text{Sec}[1 - e^x] \text{Tan}[1 - e^x]$$

Problem 704: Result more than twice size of optimal antiderivative.

$$\int \frac{e^{3x}}{-1 + e^{2x}} dx$$

Optimal (type 3, 10 leaves, 3 steps):

$$e^x - \text{ArcTanh}[e^x]$$

Result (type 3, 26 leaves):

$$e^x + \frac{1}{2} \text{Log}[1 - e^x] - \frac{1}{2} \text{Log}[1 + e^x]$$

Problem 720: Result more than twice size of optimal antiderivative.

$$\int \frac{1}{-e^{-x} + e^x} dx$$

Optimal (type 3, 6 leaves, 2 steps):

$$-\text{ArcTanh}[e^x]$$

Result (type 3, 23 leaves):

$$\frac{1}{2} \text{Log}[1 - e^x] - \frac{1}{2} \text{Log}[1 + e^x]$$

Problem 728: Result more than twice size of optimal antiderivative.

$$\int \frac{1}{-e^x + e^{3x}} dx$$

Optimal (type 3, 12 leaves, 3 steps):

$$e^{-x} - \text{ArcTanh}[e^x]$$

Result (type 3, 32 leaves):

$$e^{-x} + \frac{1}{2} \text{Log}[1 - e^{-x}] - \frac{1}{2} \text{Log}[1 + e^{-x}]$$

Problem 767: Unable to integrate problem.

$$\int e^{a+c+bx^n+dx^n} dx$$

Optimal (type 4, 37 leaves, 2 steps):

$$\frac{e^{a+c} x \left(- (b+d) x^n \right)^{-1/n} \text{Gamma} \left[\frac{1}{n}, - (b+d) x^n \right]}{n}$$

Result (type 8, 17 leaves):

$$\int e^{a+c+bx^n+dx^n} dx$$

Problem 768: Unable to integrate problem.

$$\int f^{a+bx^n} g^{c+dx^n} dx$$

Optimal (type 4, 50 leaves, 2 steps):

$$\frac{f^a g^c x \text{Gamma} \left[\frac{1}{n}, -x^n (b \text{Log}[f] + d \text{Log}[g]) \right] \left(-x^n (b \text{Log}[f] + d \text{Log}[g]) \right)^{-1/n}}{n}$$

Result (type 8, 21 leaves):

$$\int f^{a+bx^n} g^{c+dx^n} dx$$

Problem 771: Unable to integrate problem.

$$\int e^{(a+bx)^n} (a+bx)^m dx$$

Optimal (type 4, 52 leaves, 1 step):

$$\frac{(a+bx)^{1+m} \left(- (a+bx)^n \right)^{-\frac{1+m}{n}} \text{Gamma} \left[\frac{1+m}{n}, - (a+bx)^n \right]}{bn}$$

Result (type 8, 19 leaves):

$$\int e^{(a+bx)^n} (a+bx)^m dx$$

Problem 772: Unable to integrate problem.

$$\int f^{(a+bx)^n} (a+bx)^m dx$$

Optimal (type 4, 56 leaves, 1 step):

$$- \frac{(a + b x)^{1+m} \text{Gamma}\left[\frac{1+m}{n}, -(a + b x)^n \text{Log}[f]\right] (- (a + b x)^n \text{Log}[f])^{-\frac{1+m}{n}}}{b n}$$

Result (type 8, 19 leaves):

$$\int f^{(a+bx)^n} (a+bx)^m dx$$

Problem 773: Unable to integrate problem.

$$\int e^{(a+bx)^3} x dx$$

Optimal (type 4, 80 leaves, 4 steps):

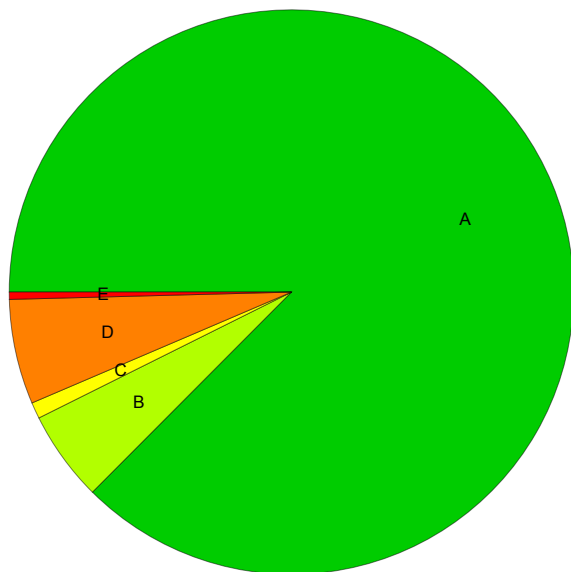
$$\frac{a (a + b x) \text{Gamma}\left[\frac{1}{3}, -(a + b x)^3\right]}{3 b^2 \left(- (a + b x)^3\right)^{1/3}} - \frac{(a + b x)^2 \text{Gamma}\left[\frac{2}{3}, -(a + b x)^3\right]}{3 b^2 \left(- (a + b x)^3\right)^{2/3}}$$

Result (type 8, 13 leaves):

$$\int e^{(a+bx)^3} x dx$$

Summary of Integration Test Results

965 integration problems



A - 844 optimal antiderivatives

B - 50 more than twice size of optimal antiderivatives

C - 9 unnecessarily complex antiderivatives

D - 58 unable to integrate problems

E - 4 integration timeouts